

# VECTORIAL HARMONICS: FROM LINK OF FRAMES TO STELLAR KINEMATICS

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## 1. OUTLINE OF THE METHOD

In astrometry, the vectorial spherical functions were used for the first time for determination of the orientation and spin between the FK5 and HIPPARCOS reference frames [1]. The present paper is devoted to elaboration of this approach to the kinematical analysis of the proper motions.

Let the proper motions in galactic coordinate system be  $\mu_l(l, b) \cos b$  and  $\mu_b(l, b)$ . We are looking for decomposition of the proper motions in such a way that

$$\mu_l(l, b) \cos b \vec{e}_l + \mu_b(l, b) \vec{e}_b = \sum_{j=1}^{\infty} [t_j \vec{T}_j(l, b) + s_j \vec{S}_j(l, b)], \quad (1)$$

where  $\vec{e}_l$  and  $\vec{e}_b$  are the unit vectors in the directions of longitude and latitude, and  $\vec{T}_j(l, b)$  and  $\vec{S}_j(l, b)$  are given in [1].

In case of the Ogorodnikov–Milne model [2] the stellar velocity field is given by expression

$$\vec{V} = \vec{V}_0 + M^+ \vec{r} + M^- \vec{r}, \quad (2)$$

where the following notations are used:

$\vec{V}_0$  — the velocity of the Sun with respect to given centroid of stars. This velocity is defined by components  $U, V, W$  in the directions of the principal galactic axes  $x, y, z$ ;

$M^+$  — the diverging matrix with the dilation coefficients  $M_{11}^+, M_{22}^+, M_{33}^+$ , and  $M_{12}^+, M_{13}^+, M_{23}^+$  standing for shears in the galactic planes  $(x, y), (x, z), (y, z)$ . Since proper motions reflect tangential motions only, we set  $M_{22}^+ = 0$ . In this case the unknowns  $M_{11}^+$  and  $M_{33}^+$  are replaced with  $M_{11}^* = M_{11}^+ - M_{22}^+$  and  $M_{33}^* = M_{33}^+ - M_{22}^+$  respectively;

$M^-$  — the rotation matrix with the components  $\omega_1, \omega_2, \omega_3$  about axes  $x, y, z$ ;

The crucial point of our method is that the elements of  $M^+$  and  $M^-$  are connected to the low-order coefficients of the decomposition (1) by the following equations (with  $R_j$  standing for the normalization factor of corresponding vectorial harmonic  $\vec{T}_j$  or  $\vec{S}_j$ ):

$$t_1 = \frac{\omega_3}{R_1}, \quad t_2 = \frac{\omega_2}{R_2}, \quad t_3 = \frac{\omega_1}{R_3}, \quad (3)$$

$$s_4 = \frac{M_{33}^* - \frac{1}{2}M_{11}^*}{2R_4}, \quad (4)$$

$$s_5 = \frac{M_{23}^+}{R_5}, \quad s_6 = \frac{M_{13}^+}{R_6}, \quad (5)$$

$$s_7 = \frac{M_{12}^+}{2R_7}, \quad s_8 = \frac{M_{11}^*}{4R_8}, \quad (6)$$

whereas the rest of harmonics does not belong to the Ogorodnikov–Milne model and may be used to study the effects that are beyond the model.

## 2. “EXTRA-MODEL” COMPONENTS OF THE PROPER MOTIONS

When applied to stellar kinematics of HIPPARCOS catalogue, the main advantage of the vectorial harmonics over traditional approach is a chance to detect the motions which are not included in the Ogorodnikov–Milne model. Indeed, in the global solution the method of vectorial functions detected the terms  $(-12.9 \pm 4.6) \times \vec{S}_{10}$ ,  $(12.2 \pm 4.4) \times \vec{S}_{14}$ ,  $(-12.7 \pm 4.6) \times \vec{S}_{20}$ ,  $(11.1 \pm 4.3) \times \vec{S}_{34}$  (all in  $\text{km s}^{-1} \text{ kps}^{-1}$ ). Besides the global solution we applied our method to several samples of stars with different distances and spectral classes. The “extra-model” terms specified by the functions  $\vec{T}_4$ ,  $\vec{T}_6$ ,  $\vec{S}_{10}$  and  $\vec{S}_{14}$  were found to be common to all examined samples including the global solution.

In conclusion, we state that contribution of the “extra-model” components to the proper motions is comparable with the contribution of the “classical” terms (see Figure 1). The next paper will be devoted to the physical properties of the “extra-model” terms detected here.

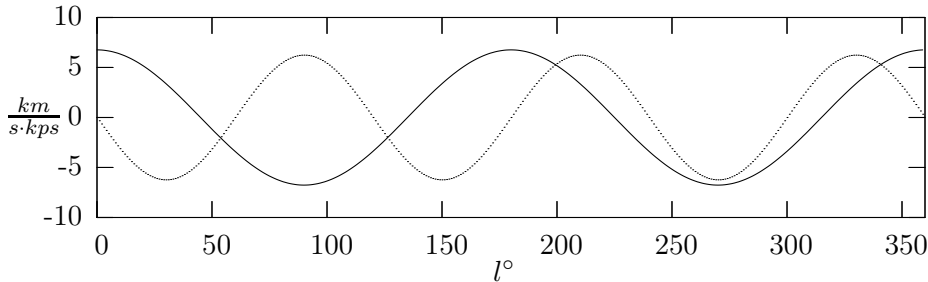


Figure 1: Contribution to the proper motions in longitude from the model harmonic  $\vec{S}_7$  (Oort’s coefficient  $A = M_{12}^+$ , solid line) in comparison to the significant “extra-model” harmonic  $\vec{S}_{14}$  (dashed line).

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## REFERENCES

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