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Aberration in proper motions for Galactic stars

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Ref: *Mon. Not. Roy. Astron. Soc.* (2013), Vol. 433, 3597–3604



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Outline

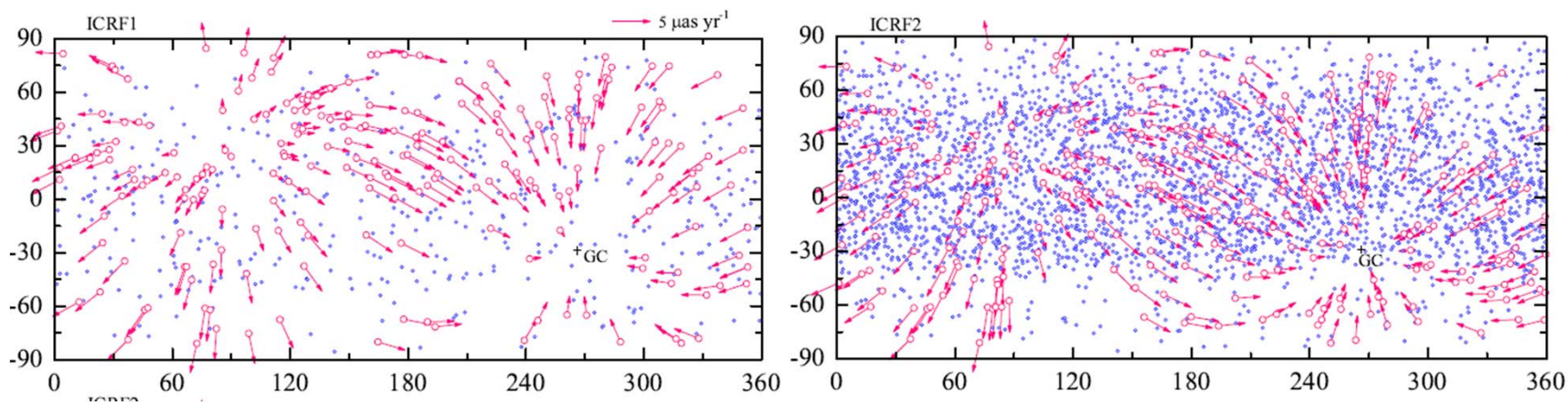
- ❑ Acceleration of the SSB and aberration in proper motions
- ❑ Theoretical expressions
- ❑ More suitable formulas for short periodic stars
- ❑ Discussion



Introduction

- ◆ Origin: acceleration of the SSB, known as secular/Galactic aberration (drift) for extragalactic sources
- ◆ Dipolar proper motions and its impact on ICRF and EOP

Ref: Liu J.-C., Capitaine N., Lambert S. Malkin Z. Zhu Z. (2012), A&A, 548, A50



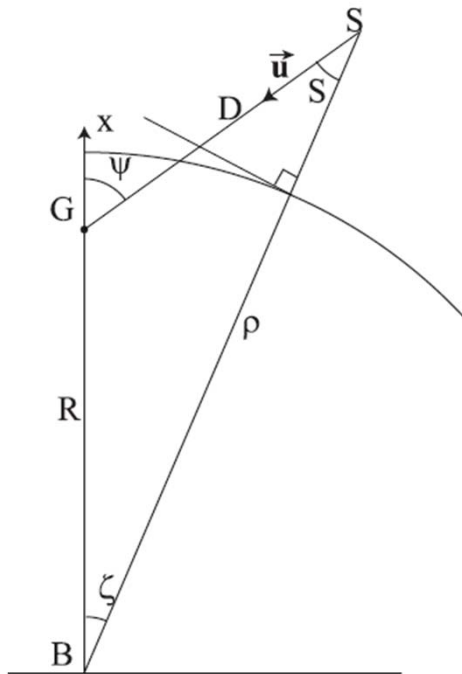
- ◆ Rotation of the ICRS: $0.1 \mu\text{as yr}^{-1} < \omega_{xyz} < 1 \mu\text{as yr}^{-1}$ depending on the distribution of sources



◆ J. Kovalevsky, *Aberration in proper motions*, 2003, A&A, 404, 743

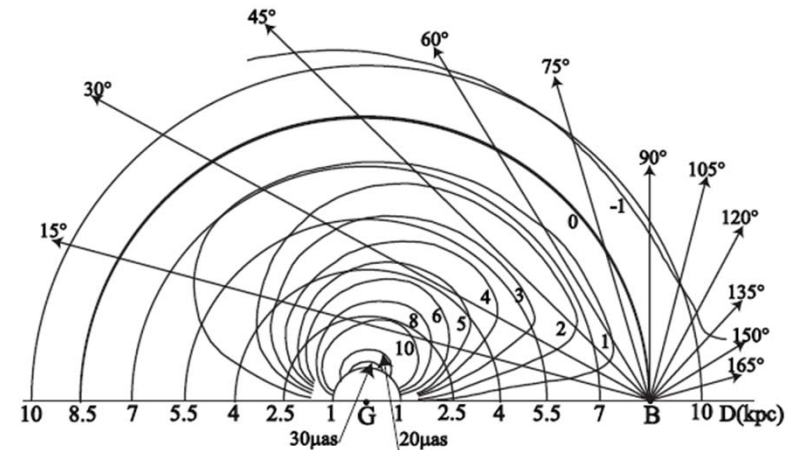
◆ Sec. 7. Time dependent aberration of stars in the Galaxy

◆ Basic assumption: central Newtonian force toward the GC



Apparent proper motions of stars

$$\Delta\mu_s = \frac{-V_c^2 R \sin \zeta}{c(R^2 + \rho^2 - 2R\rho \cos \zeta)}$$





Theoretical Expressions

Planetary aberration in positions

$$\Delta \mathbf{p}^{\text{PL}} = \frac{1}{c} \mathbf{p} \times [(\mathbf{v}^{\text{E}} - \mathbf{v}^{\text{PL}}) \times \mathbf{p}]$$



Higher hierarchy
reference system

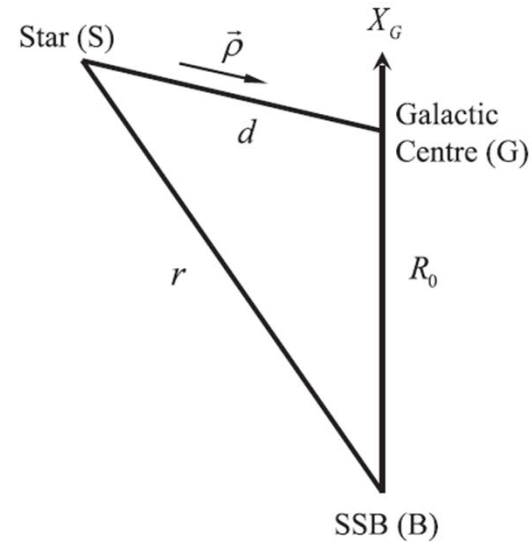
Aberration in proper motions

$$\Delta \dot{\mathbf{p}}^{\text{S}} = \frac{1}{c} \mathbf{p} \times [(\mathbf{a}^{\text{B}} - \mathbf{a}^{\text{S}}) \times \mathbf{p}]$$

Apparent proper motions in Galactic longitude and latitude

$$\Delta \mu_{\ell} \cos b = \Delta \dot{\mathbf{p}}^{\text{S}} \cdot \mathbf{e}_{\ell} = \frac{1}{c} \mathbf{p} \times [(\mathbf{a}^{\text{B}} - \mathbf{a}^{\text{S}}) \times \mathbf{p}] \cdot \mathbf{e}_{\ell}$$

$$\Delta \mu_b = \Delta \dot{\mathbf{p}}^{\text{S}} \cdot \mathbf{e}_b = \frac{1}{c} \mathbf{p} \times [(\mathbf{a}^{\text{B}} - \mathbf{a}^{\text{S}}) \times \mathbf{p}] \cdot \mathbf{e}_b,$$



Galactic aberration constant for the SSB

$$A^{\text{B}} = \frac{a^{\text{B}}}{c} = \frac{V_0^2}{cR_0} \simeq 5 \mu\text{as yr}^{-1} \quad \text{Session 1 poster by Z. Malkin.}$$

and define:

$$\gamma = \frac{a^{\text{S}}}{a^{\text{B}}}$$

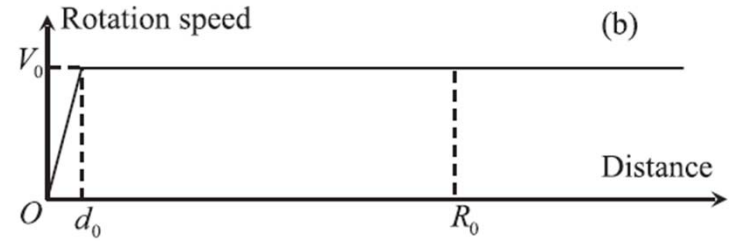
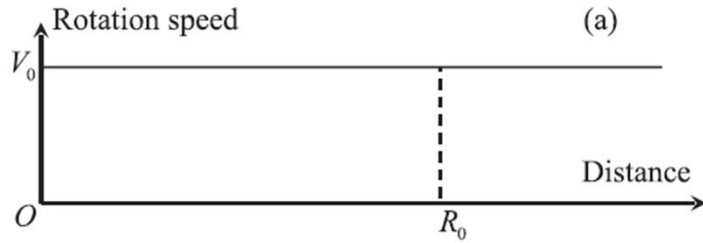
$$= -A^{\text{B}} \left(1 - \gamma \frac{R_0}{d}\right) \sin \ell$$



$$= -A^{\text{B}} \left(1 - \gamma \frac{R_0}{d}\right) \cos \ell \sin b$$



Simplified rotation curve of the Galactic disk

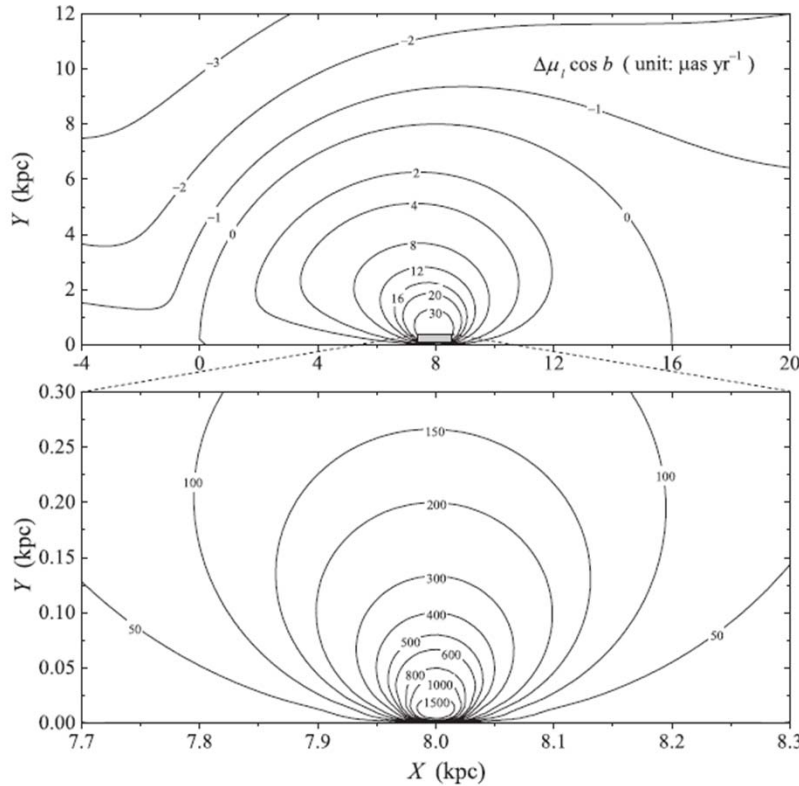
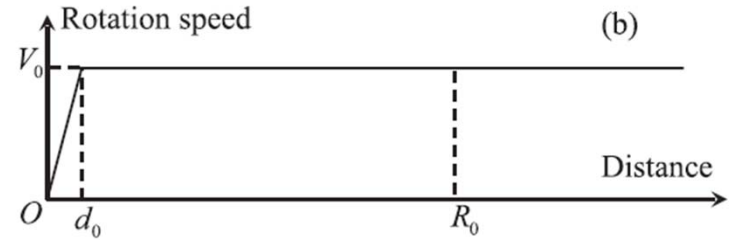
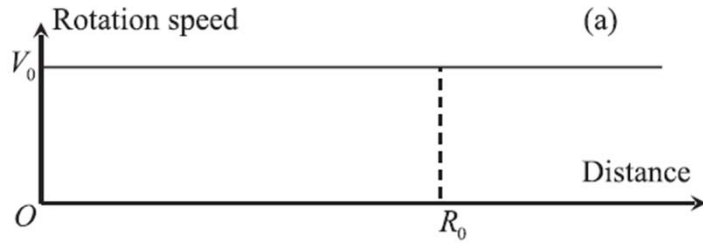


$$\gamma = \frac{R_0}{d} \rightarrow \begin{cases} \Delta\mu_\ell \cos b = -A^B \left[1 - \left(\frac{R_0}{d} \right)^2 \right] \sin \ell \\ \Delta\mu_b = -A^B \left[1 - \left(\frac{R_0}{d} \right)^2 \right] \cos \ell \sin b. \end{cases}$$

$$\gamma = \frac{R_0 d}{d_0^2} \rightarrow \begin{cases} \Delta\mu_\ell \cos b = -A^B \left[1 - \left(\frac{R_0}{d_0} \right)^2 \right] \sin \ell \\ \Delta\mu_b = -A^B \left[1 - \left(\frac{R_0}{d_0} \right)^2 \right] \cos \ell \sin b \end{cases}$$



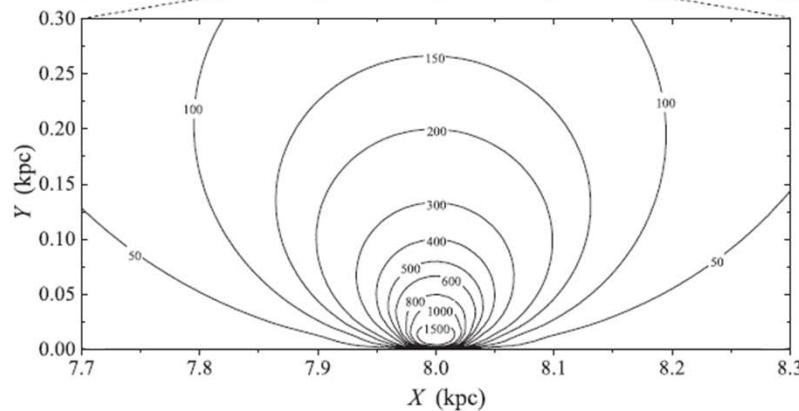
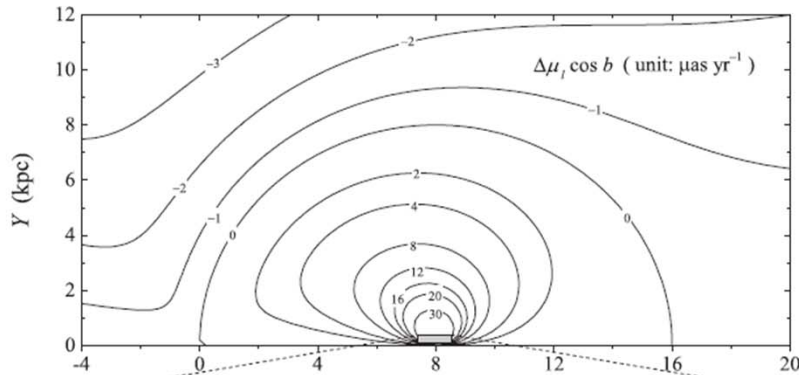
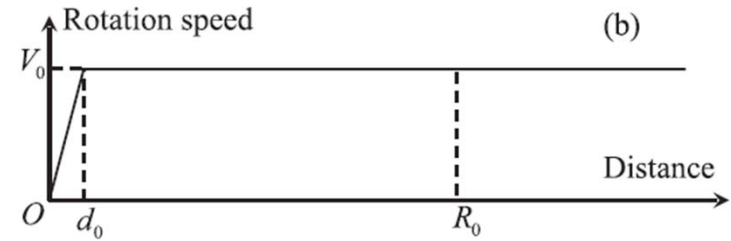
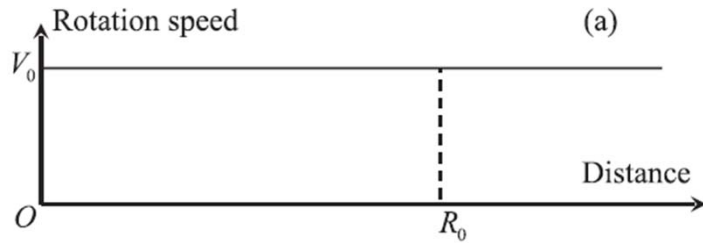
Simplified rotation curve of the Galactic disk



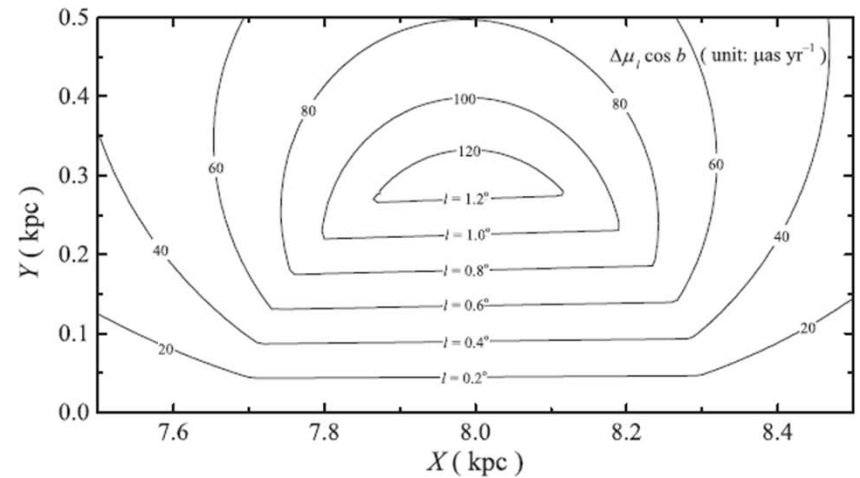
$$\gamma = \frac{R_0 d}{d_0^2} \rightarrow \begin{cases} \Delta\mu_\ell \cos b = -A^B \left[1 - \left(\frac{R_0}{d_0} \right)^2 \right] \sin \ell \\ \Delta\mu_b = -A^B \left[1 - \left(\frac{R_0}{d_0} \right)^2 \right] \cos \ell \sin b \end{cases}$$



Simplified rotation curve of the Galactic disk



$$\gamma = \frac{R_0 d}{d_0^2} \rightarrow \begin{cases} \Delta\mu_\ell \cos b = -A^B \left[1 - \left(\frac{R_0}{d_0} \right)^2 \right] \sin \ell \\ \Delta\mu_b = -A^B \left[1 - \left(\frac{R_0}{d_0} \right)^2 \right] \cos \ell \sin b \end{cases}$$





The light travel time issue

- ◆ Approximation in the basic equation $\Delta \dot{p}^S = \frac{1}{c} p \times [(a^B - a^S) \times p]$ (*)
- ◆ How to deal with non-rectilinear acceleration during the light travel time from the star to the observer?

Define the ratio of the orbital period and the light time τ .

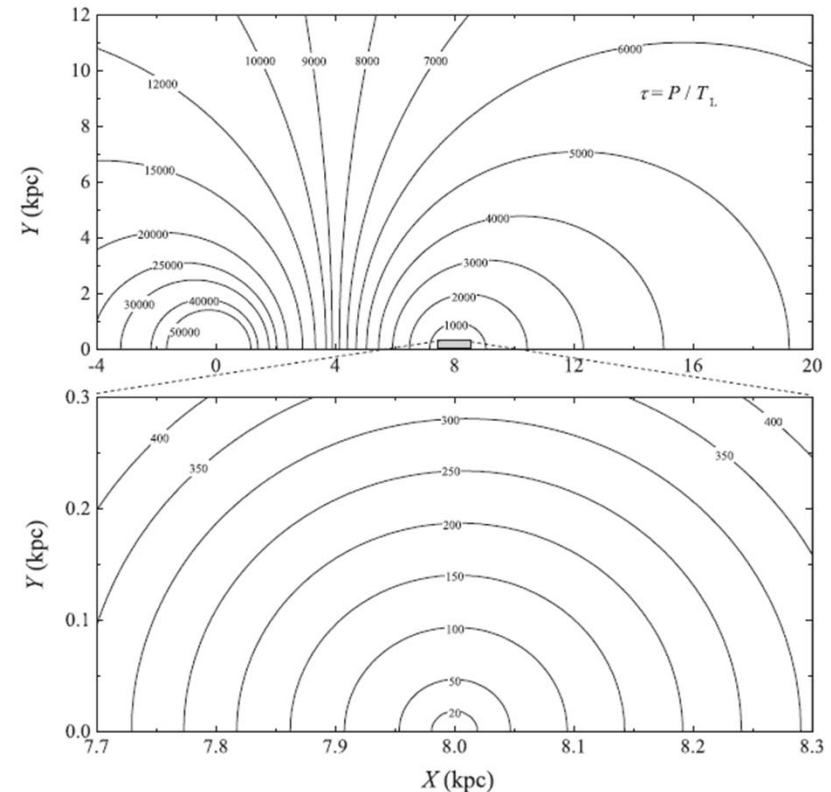
$\tau \gg 1$ means (*) is appropriate.

Flat rotation curve:

$$\tau = \frac{P}{T_L} = 2\pi \left(\frac{d}{r} \right) \left(\frac{c}{V^S} \right) \quad \longrightarrow$$

Within the bulge region

$$\tau \simeq 320 \quad (d < d_0 = 0.3 \text{ kpc})$$



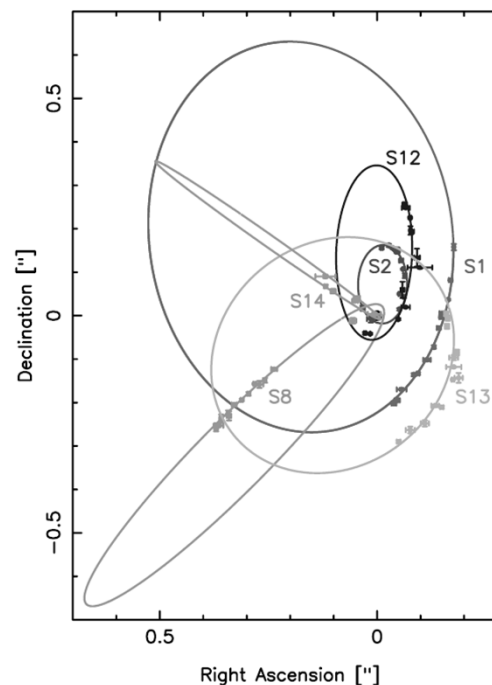


Example: S2 star near the central black hole.

Table A1. Elements of the Keplerian orbit of S0-2.

Element of the orbit	Value	Unit
Central mass	3.3 ± 0.7	$10^6 M_{\odot}$
Semimajor axis	4.54 ± 0.27	10^{-3} pc
Separation of pericentre	0.59 ± 0.10	10^{-3} pc
Eccentricity	0.87 ± 0.02	–
Period	15.73 ± 0.74	yr
Pericentre passage	2002.31 ± 0.02	yr
Inclination	45.7 ± 2.60	degree
Angle of line of nodes	44.2 ± 7.0	degree
Angle of node of pericentre	244.7 ± 4.7	degree

Note: The table is grabbed from table 4 of Schödel et al. (2003).



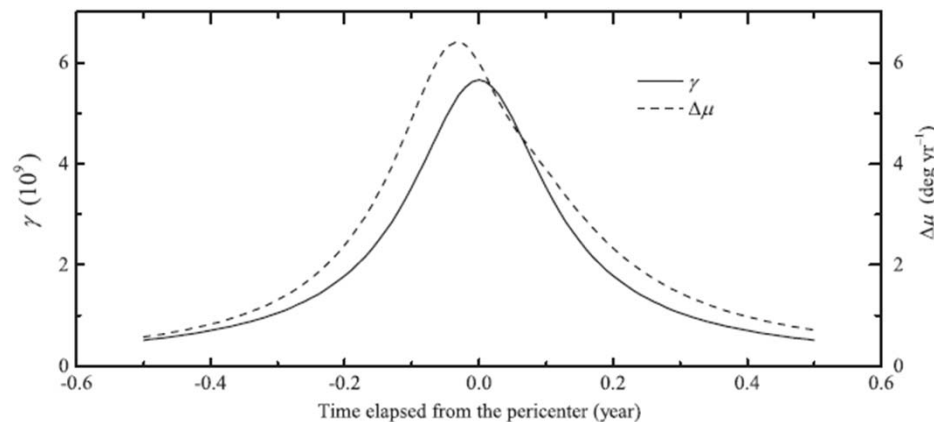
Light time from S2 to the SSB:

$$T_L \simeq 8000 \text{ pc} \times 3.26 \text{ yr pc}^{-1} = 26000 \text{ yr},$$

Apparent proper motions:

$$\Delta\mu_{\alpha} \cos \delta \simeq a^S T_L \frac{\Delta x}{d} \frac{1}{R_0}$$

$$\Delta\mu_{\delta} \simeq a^S T_L \frac{\Delta y}{d} \frac{1}{R_0}$$



unrealistic large proper motions



A more suitable expression

- ◆ The previous equation may be inappropriate for short periodic stars
- ◆ Integer multiple of periods: the aberrational effect is zero
- ◆ *Define:* P_f = remainder of T_L divided by P

- ◆ *Effective aberration in proper motions:*
$$\Delta \dot{p}^S = \frac{1}{c} p \times \left[\left(a^B - \frac{v_2^S - v_1^S}{T_L} \right) \times p \right]$$

Apparent proper motions:
$$\Delta \mu_\alpha \cos \delta = \frac{1}{\kappa} \frac{v_{2,x} - v_{1,x}}{r}, \quad \Delta \mu_\delta = \frac{1}{\kappa} \frac{v_{2,y} - v_{1,y}}{r}$$

True proper motions at t_1 :
$$[\Delta \mu_\alpha \cos \delta]_1^{\text{true}} = \frac{1}{\kappa} \frac{v_{1,x}}{r}, \quad [\Delta \mu_\delta]_1^{\text{true}} = \frac{1}{\kappa} \frac{v_{1,y}}{r}$$



Observed proper motions at t_1 :

$$[\Delta\mu_\alpha \cos \delta]_1^{\text{obs}} = \frac{1}{\kappa} \frac{v_{2,x}}{r} = [\Delta\mu_\alpha \cos \delta]_2^{\text{true}}$$

$$[\Delta\mu_\delta]_1^{\text{obs}} = \frac{1}{\kappa} \frac{v_{2,y}}{r} = [\Delta\mu_\delta]_2^{\text{true}}.$$

$P_f \ll T_L$:

- ◆ The effect of aberration will have no effect on the shape of the orbit
 - ◆ Only change the observed phase of stars on the orbit
-

Systematic effect on the Gaia stellar reference frame

- ◆ Global rotation: larger than the effect of Galactic aberration (μas level)
- ◆ Small distortion also exists.
- ◆ Important in the GaiaCRF?



Discussion

- ◆ Non-disk stars (halo, bulge)
- ◆ More realistic model of Galactic kinematics is necessary.
- ◆ Observable? (Embedded in stellar proper motions.)
- ◆ Kovalevsky (2003): “Applying this correction corresponds to changing from the Barycentric Celestial Reference Frame (BCRS) to a Galactocentric Celestial Reference Frame (GalCRS).”
- ◆ The nomenclature issue for relevant effects.

Thank you!

