# APPLICATIONS OF SIMULTANEOUS GROUND-BASED AND SATELLITE OBSERVATIONS 

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#### Abstract

Simultaneous ground-based and satellite observations either of a body of the solar system or an external source, together with mutual observations between satellite and Earth observational sites could be used to monitor different reference systems.


## 1. GENERAL DESCRIPTION OF THE METHOD

We consider $F$ and $f$, the functionals to optimize, where $f$ depends on the following set of parameters: the terrestrial physical $\pi_{\phi}$, the geometrical of the terrestrial system $\pi_{E}$ and the geometrical of the considered system (for example, a net of artificial satellites) $\pi_{S}$. Analogously, the functional $F$ also includes, implicitly, parameters related to the terrestrial motion in the inertial system $\Pi_{E}$, geometrical of the terrestrial system $\pi_{E}$ and also physical $\pi_{\phi}$. From the initial values $\pi_{\phi}^{0}, \pi_{E}^{0}, \pi_{S}^{0}$ we can obtain increments $\delta \pi_{\phi}^{0}, \delta \pi_{E}^{0}, \delta \pi_{S}^{0}$ minimizing the functional $f$. The previous process provides values, which we denote as $\pi_{\phi}^{1}, \pi_{E}^{1}, \pi_{S}^{1}$ which are the result of adding to the initial values the obtained increments.
These new parameters are included in the functional $F$ where, in addition, we should consider the increments $\delta \pi_{\phi}^{1}, \delta \pi_{E}^{1}, \delta \Pi_{E}^{0}+\delta \Pi_{E}^{1}$ where we have usually a relationship between $\delta \pi_{\phi}^{0}$ and $\delta \Pi_{E}^{0}$, through a expression $g\left(\delta \Pi_{E}^{0}\right)=\delta \pi_{\phi}^{0}$. Then, we optimize the other functional $F$ to obtain the corresponding corrections and then we return to the functional $f$ until we obtain stationary values in the parameters. To summarize, we consider a precision previously fixed, $\varepsilon>0$ and the process may be described as:

Opt $F\left(\Pi_{E}^{[i]}+\delta \Pi_{E}^{i+1}, \pi_{E}^{i+1}+\delta \pi_{E}^{i+1}, \pi_{\phi}^{i+1}\right)$ subject to
Opt $f\left(\pi_{\phi}^{i}+\delta \pi_{\phi}^{i}, \pi_{E}^{i}+\delta \pi_{E}^{i}, \pi_{S}^{i}+\delta \pi_{S}^{i}\right)$
$g\left(\delta \pi_{\phi}^{i}\right)=\delta \Pi_{E}^{i}$
$\Pi_{E}^{[i]}=\Pi_{E}^{i}+\delta \Pi_{E}^{i}$
Stop if $\left\|\left(\delta \pi_{\phi}^{i}, \delta \pi_{E}^{i}, \delta \pi_{S}^{i}, \delta \Pi_{E}^{i}\right)\right\|_{\infty}<\varepsilon$
on the contrary
put $\Pi_{E}^{i+1}=\Pi_{E}^{[i]}, \pi_{E}^{i+1}=\pi_{E}^{i}+\delta \pi_{E}^{i}, \pi_{\phi}^{i+1}=\pi_{\phi}^{i}+\delta \pi_{\phi}^{i}$ and
Continue
We should remark that each problem usually includes the optimization (generally minimization) of a different discrete either continuous functional, defined by means of a succession of temporal data either a spatial distribution either both cases. In any case, the traditional methods of optimization (quadratic minimization) do not necessary work. We should pay a special attention to the distribution of the available data. Some particular cases are now been studied by the authors.

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