

POLISH
ACADEMY
OF SCIENCES

SPACE
RESEARCH
CENTRE

Journées 2005

Systèmes de Référence Spatio-Temporels

*"Earth dynamics and reference systems:
five years after the adoption
of the IAU 2000 Resolutions"*

Warsaw, 19-21 September 2005



Progress on the Implementation of the New Nomenclature in The Astronomical Almanac

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The Astronomical Almanac & *The Astronomical Almanac Online*



Joint publication of USNO & HMNAO

- Reference product for the year
- Useful to the people who need the information
- Must maintain international “standards” — up to date & reliable
- 2006 edition available since Jan 2005 — **first** edition with IAU 2000 & new nomenclature
- **2007 in preparation** — to press October 1, 2005



The AsA & The AsA Online



USNO – sections

- C – Sun
- E – Planets
- F – Satellites
- H – Stars
- L – Glossary
- M – Notes & References

HMNAO – sections

- A – Phenomena
- B – Time scales & reference systems
- D – Moon
- G – Minor planets
- K – Reference data

Section B: Time Scales & Reference Systems

- **Software comparisons**
- **Tables**
- **Explanation**

Software Comparisons

- HMNAO

IAU-SOFA

- USNO

NOVAS

- Recommendations by WG
Precession & the Ecliptic (P03)

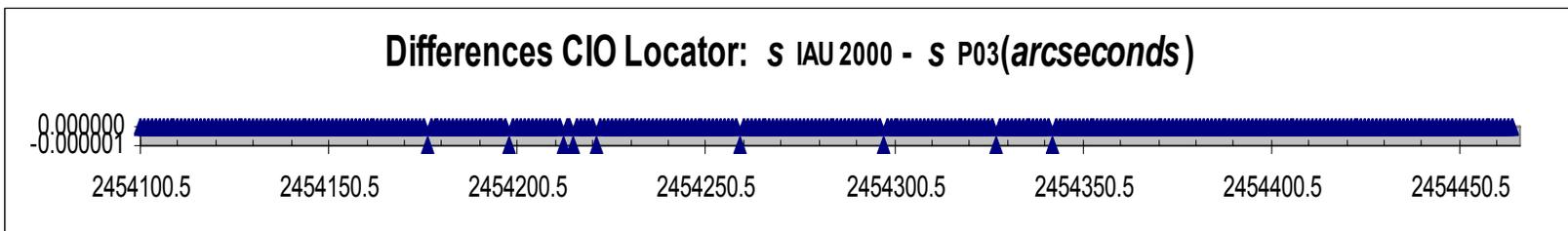
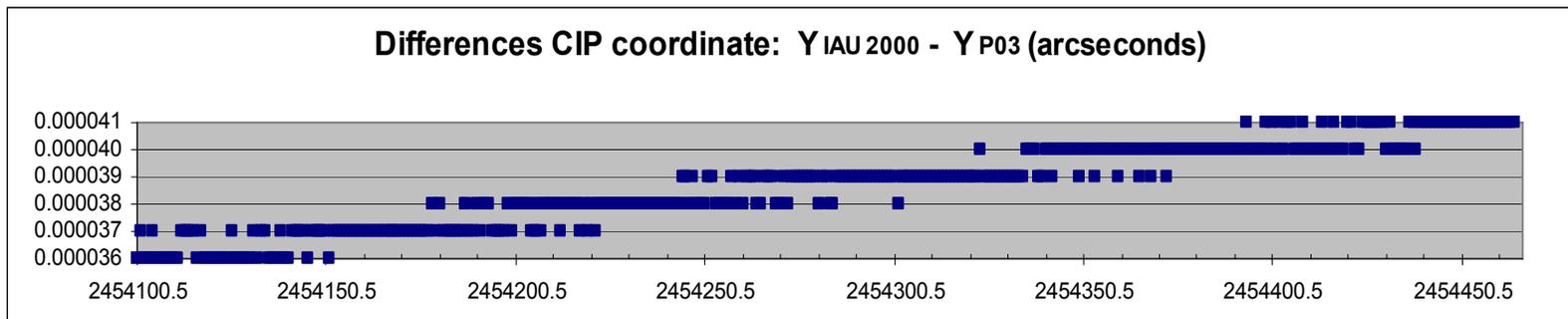
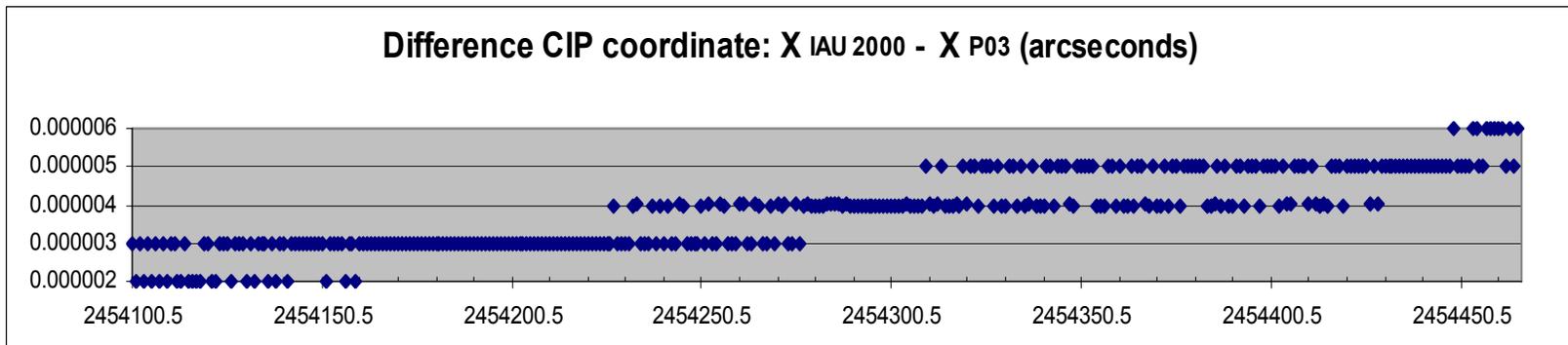
Software: P03

Recommended by IAU WG on Precession & the Ecliptic

- AsA 2007 (& 2006) do **not** use P03
 - Not yet an IAU standard
 - Not yet incorporated into SOFA
 - NOVAS (v 3) code is **already** written
 - Differences **hardly** affect the printed precision of AsA 2007.
- **AsA 2008** will use **P03** from **SOFA & NOVAS 3**

Differences: 2007, CIP & CIO Locator

IAU 2000 – P03



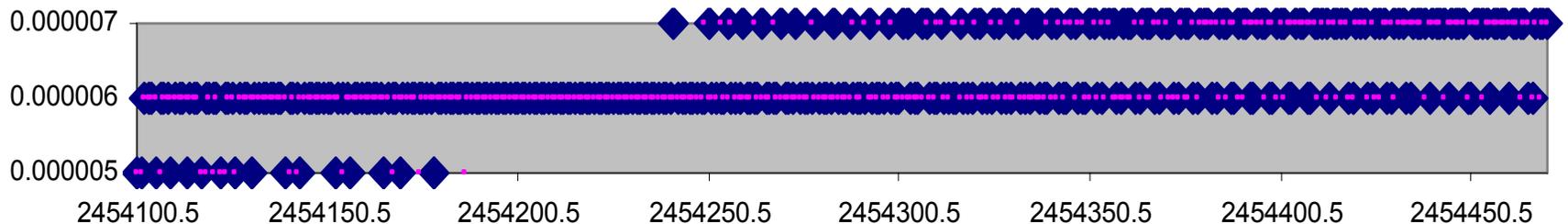
Differences: XY of CIP, CIO Locator & Obliquity IAU 2000 – P03

In units of printed precision 0.1 mas (0".0001)

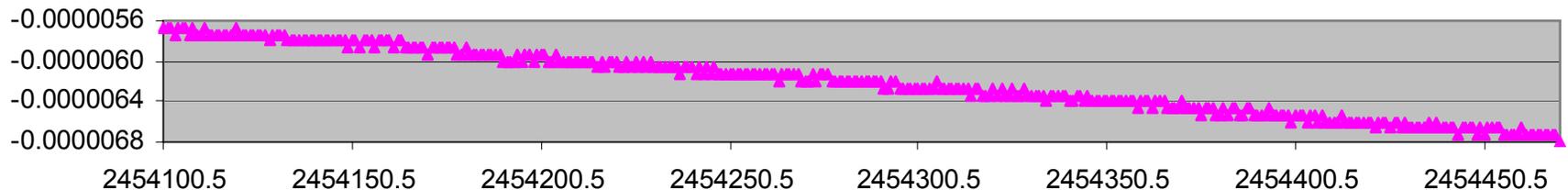
Quantity	2007 mas	2006-2008 mas
X	[0.00, +0.01]	[0.00, +0.01]
Y	[+0.04]	[+0.03, +0.05]
s	[0.00]	[0.00]
ε	[+41.7, +41.8]	[+41.7, +41.8]

Differences: 2007, GMST/GAST & E_0 IAU 2000 – P03

Differences: GMST (s) & GAST (s) 2007



Differences: Equation of the Origins (s) 2007



Differences: Greenwich Mean & Apparent Sidereal Time, Equation of the Origins IAU 2000 – P03

In units of the printed precision 0.1 ms ($0^s.0001$)

Quantity	2007 ms	2006-2008 ms
GMST/GAST	[+0.005, +0.007]	[+0.004, +0.008]
E_o	[-0.007, -0.006] mas	[-0.008, -0.005] mas
GMST/GAST	[+0.1]	[+0.1]
E_o	[-0.1]	[-0.1]

HMNAO(SOFA) v NOVAS: 2005 – 2007

1101 dates

Quantity Daily 0 ^h UT1	Unit	Decimal Places Printed	Decimal Places Checked	Number of Values 1 Different
GMST	s	4	6	0
GAST	s	4	6	1
E _E	s	4	6	0
ERA	"	4	6	0
E _O	"	4	6	224

HMNAO(SOFA) v NOVAS: 2005 – 2007

(1101 dates)

Quantity Daily 0 ^h TT	Unit	Decimal Places Printed	Decimal Places Checked	Number of Values 1 Different
$\Delta\psi$	"	4	6	3
$\Delta\varepsilon$	"	4	6	0
ε	"	4	6	0
X	"	4	6	160
Y	"	4	6	0
s^*	"	4	10	see below

* s , 2 daily, 12^hTDB, differences between $\pm 1'' \times 10^{-6}$

HMNAO(SOFA) v NOVAS: 2005 – 2007

(1101 dates x 9 elements)

Quantity Daily 0 ^h TT	Decimal Places Printed	Decimal Places Checked	Number of Values 1 Different
NPB	10	12	15%
C* (ignoring elements C ₂₁ & C ₁₂)	10	12	15%

C₂₁ & **C**₁₂ 15% were different; maximum ± 5 in the 12th place

Apparent Places, Sun, Moon, Planets:

HMNAO v NOVAS

0".001 printed precision

- Method in Section **B** \neq **NOVAS** (2.9 Beta)
 - NOVAS modern implementation & includes light deflection from planets
- **2005-2015**, daily at 0^h TT, agreement better than $9'' \times 10^{-6}$, **except**
 - **Moon**; 0".0003; limitations of double precision on the light-time iteration
 - **Uranus & Neptune**; close to Jupiter: 0".0002

Tables in Section B

- Universal & Sidereal Times
- UT, Earth rotation angle, equation of the origins
- Nutations Long., & Obl., ε , and X, Y, s
- **NPB**: the GCRS to equator and equinox matrix
- **C**: the GCRS to intermediate matrix
- Position and velocity of the Earth

B20 UNIVERSAL TIME AND EARTH ROTATION ANGLE, 2007

Date 0 ^h UT1	Julian Date	Earth Rotation Angle θ			Equation of Origins E_o		Date 0 ^h UT1	Julian Date	Earth Rotation Angle θ			Equation of Origins E_o	
	245	°	'	"	'	"		245	°	'	"	'	"
Jan. 0	4100.5	99	11	34.1541	– 5	25.6403	Feb. 15	4146.5	144	31	51.5490	– 5	33.2447
1	4101.5	100	10	42.3583	– 5	25.8980	16	4147.5	145	30	59.7532	– 5	33.4479
2	4102.5	101	09	50.5626	– 5	26.1914	17	4148.5	146	30	07.9575	– 5	33.5985
3	4103.5	102	08	58.7668	– 5	26.4943	18	4149.5	147	29	16.1617	– 5	33.6866
4	4104.5	103	08	06.9710	– 5	26.7799	19	4150.5	148	28	24.3660	– 5	33.7209
5	4105.5	104	07	15.1753	– 5	27.0274	20	4151.5	149	27	32.5702	– 5	33.7279
6	4106.5	105	06	23.3795	– 5	27.2259	21	4152.5	150	26	40.7744	– 5	33.7432
7	4107.5	106	05	31.5838	– 5	27.3749	22	4153.5	151	25	48.9787	– 5	33.7980
8	4108.5	107	04	39.7880	– 5	27.4825	23	4154.5	152	24	57.1829	– 5	33.9090
9	4109.5	108	03	47.9922	– 5	27.5620	24	4155.5	153	24	05.3871	– 5	34.0758
10	4110.5	109	02	56.1965	– 5	27.6293	25	4156.5	154	23	13.5914	– 5	34.2833
11	4111.5	110	02	04.4007	– 5	27.7006	26	4157.5	155	22	21.7956	– 5	34.5090
12	4112.5	111	01	12.6049	– 5	27.7908	27	4158.5	156	21	29.9999	– 5	34.7286
13	4113.5	112	00	20.8092	– 5	27.9126	28	4159.5	157	20	38.2041	– 5	34.9211

$$\text{GHA} = \theta - \alpha_i, \quad \alpha_i = \alpha_e + E_o$$

α_i, α_e are the right ascensions with respect to the CIO and the true equinox of date, respectively.

B34 NUTATION, OBLIQUITY & INTERMEDIATE SYSTEM, 2007

FOR 0^h TERRESTRIAL TIME

Date 0 ^h TT	NUTATION		True Obl. of Ecliptic ϵ 23° 26'	Julian Date 0 ^h TT	CELESTIAL INTERMEDIATE		
	in Long. $\Delta\psi$	in Obl. $\Delta\epsilon$			Pole X	Y	Origin S
	"	"	"		"	"	"
Jan. 0	+ 3.1893	+ 8.3914	26.5622	4100.5	+ 141.4879	+ 8.2711	- 0.0020
1	+ 3.3325	+ 8.3471	26.5166	4101.5	+ 141.5996	+ 8.2267	- 0.0020
2	+ 3.5146	+ 8.3248	26.4930	4102.5	+ 141.7269	+ 8.2041	- 0.0020
3	+ 3.7071	+ 8.3297	26.4966	4103.5	+ 141.8584	+ 8.2088	- 0.0020
4	+ 3.8808	+ 8.3605	26.5261	4104.5	+ 141.9824	+ 8.2394	- 0.0020
5	+ 4.0129	+ 8.4103	26.5747	4105.5	+ 142.0899	+ 8.2891	- 0.0020
6	+ 4.0917	+ 8.4693	26.6324	4106.5	+ 142.1762	+ 8.3479	- 0.0020
7	+ 4.1165	+ 8.5272	26.6890	4107.5	+ 142.2411	+ 8.4057	- 0.0020
8	+ 4.0962	+ 8.5755	26.7360	4108.5	+ 142.2880	+ 8.4539	- 0.0021
9	+ 4.0453	+ 8.6083	26.7676	4109.5	+ 142.3226	+ 8.4867	- 0.0021

GCRS to Equator of Date Matrices

B42 FRAME BIAS, PRECESSION AND NUTATION, 2007

MATRIX ELEMENTS FOR CONVERSION FROM
GCRS TO TRUE EQUATOR AND EQUINOX OF DATE
FOR 0^h TERRESTRIAL TIME

Date 0 ^h TT	NPB ₁₁ -1	NPB ₁₂	NPB ₁₃	NPB ₂₁	NPB ₂₂ -1	NPB ₂₃	NPB ₃₁	NPB ₃₂	NPB ₃₃ -1
Jan. 0	-14815	-1578 7515	- 685 8885	+1578 7236	-12470	-41 1824	+ 685 9526	+40 0995	-2361
1	-14838	-1580 0005	- 686 4306	+1579 9728	-12490	-40 9686	+ 686 4945	+39 8840	-2364
2	-14865	-1581 4229	- 687 0478	+1581 3952	-12512	-40 8613	+ 687 1116	+39 7747	-2369
3	-14892	-1582 8915	- 687 6851	+1582 8638	-12536	-40 8860	+ 687 7490	+39 7975	-2373
4	-14918	-1584 2762	- 688 2860	+1584 2483	-12558	-41 0363	+ 688 3502	+39 9458	-2377

FRAME BIAS, PRECESSION AND NUTATION, 2007

B43

MATRIX ELEMENTS FOR CONVERSION FROM
GCRS TO CELESTIAL INTERMEDIATE ORIGIN & TRUE EQUATOR OF DATE
FOR 0^h TERRESTRIAL TIME

Julian Date	C ₁₁ -1	C ₁₂	C ₁₃	C ₂₁	C ₂₂ -1	C ₂₃	C ₃₁	C ₃₂	C ₃₃ -1
245									
4100.5	- 2353	- 40	- 685 9526	- 235	- 8	-40 0995	+ 685 9526	+40 0995	- 2361
4101.5	- 2356	- 40	- 686 4945	- 233	- 8	-39 8840	+ 686 4945	+39 8840	- 2364
4102.5	- 2361	- 41	- 687 1116	- 233	- 8	-39 7747	+ 687 1116	+39 7747	- 2369
4103.5	- 2365	- 41	- 687 7490	- 233	- 8	-39 7975	+ 687 7490	+39 7975	- 2373
4104.5	- 2369	- 41	- 688 3502	- 234	- 8	-39 9458	+ 688 3502	+39 9458	- 2377

Explanation

- Corrected some mistakes
- Improved explanation
- ICRS/BCRS/GCRS
- Date – JD_{TT} , JD_{UT}
- Nomenclature, in line with WG recommendations
- Included the precession matrix using χ , ψ , ω , ε_0
- Made the pages less full – a few more pages

Approximate GCRS to CIO & Equator of Date, Valid for a Year (0".3) : 2007

$$X = 140''.20 + 0.0549 d - 6.8 \sin \Omega - 0.5 \sin 2L$$

$$Y = -0''.12 + 9.2 \cos \Omega + 0.6 \cos 2L$$

$$\mathbf{C} = \begin{pmatrix} 1 & -X^2/2 & 0 & -X \\ 0 & 1 & -Y \\ X & Y & 1 & -X^2/2 \end{pmatrix}$$

Exclude X^2 term: 2014 error in Dec increased to +/-0".4

2025 error in Dec increased to +/-0".7

Summary: Calculate GHA & δ

1. **GCRS**: calculate geocentric vector, apply corrections for light-time, light deflection, aberration as appropriate;
2. **Rotations**: transform **GCRS** to required “of date” system;

Equinox-based

- A. Apply **NPB** to give the true equinox and equator of date,
- B. Apply GAST.

OR

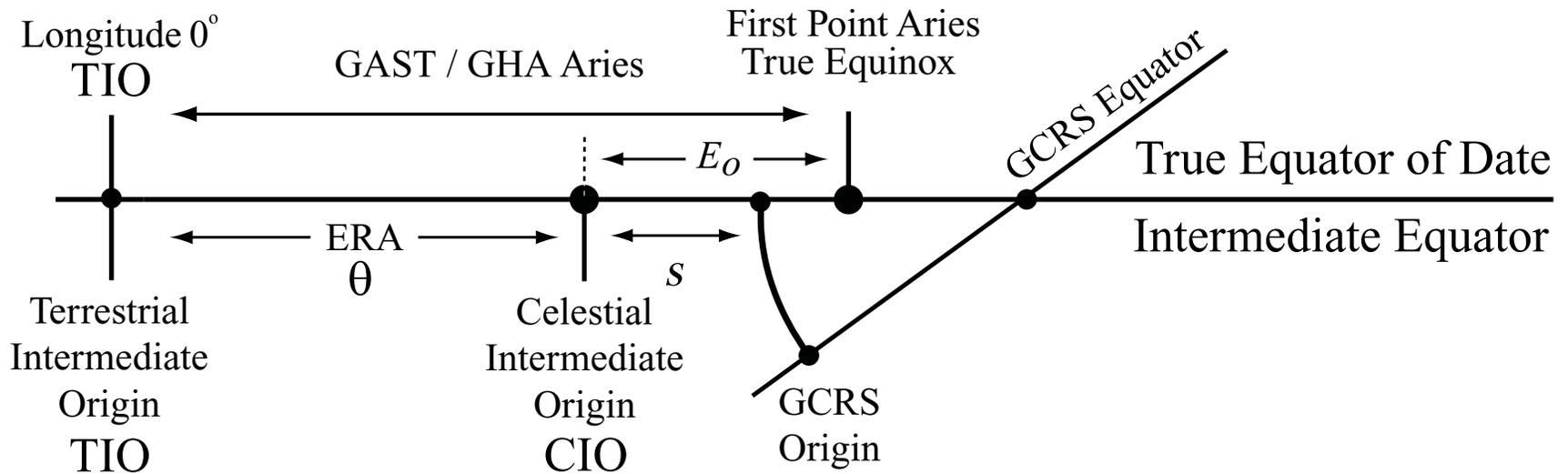
CIO-based

- A. Apply **C**(X, Y, s) to give Celestial Intermediate Reference System,
- B. Apply ERA.

3. **Calculate** hour angle (GHA) and declination (δ).

Summary

Relationship between GAST & ERA



Schematic Diagram

Summary of Nomenclature

Equinox Based

- True Equator & Equinox of date
 - CIP (X, Y)
 - True equator of date
 - True equinox of date
 - Apparent place
 - Apparent RA
 - Declination
- GAST
- Hour angle

CIO Based

- Celestial Intermediate Reference System
 - CIP (X, Y)
 - Celestial Intermediate Equator
 - CIO – located using s
 - Intermediate place
 - Intermediate RA
 - Declination
- ERA
- Hour angle

IAU 2000 (2006) Resolutions Explained

- USNO Circular 179 by George Kaplan
<http://aa.usno.navy.mil/kaplan/Circular.html>
- Printed version available in December 2005

