

# *The IAU Recommendations on Reference Systems and their Applications*

Nicole Capitaine, Observatoire de Paris, France

Dennis D. McCarthy, U.S. Naval Observatory

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## *Why?*

- Previous definitions were not precise at the level of  $\mu$ seconds of arc
- Improved geophysical nutation model delivered by IAU/IUGG Working Group
- Defining astronomical observations not sensitive to the ecliptic

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## IAU Resolutions for the Celestial Reference System

**IAU GA 1988** extragalactic objects to define the celestial reference frame,

### IAU GA 1991

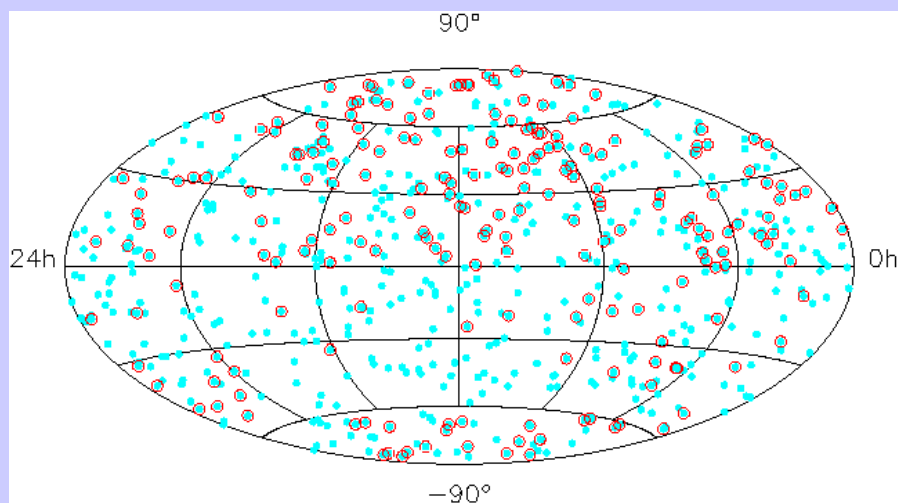
- adopts GR as the fundamental theory
- specifies continuity with existing stellar and dynamic realizations,

### IAU GA 1997

- from 1 January 1998, the IAU celestial reference system is the **International Celestial Reference System (ICRS)**
- corresponding fundamental reference frame is the **International Celestial Reference Frame (ICRF)**

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## The ICRF



Adopted as the International Celestial Reference System by the IAU  
(1st January 2003)

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## Change from FK5 catalog to ICRF

### - FK5 -

- realized by positions and proper motions of bright stars

*(precision : 20 mas, 80 mas/c)*

- positions and proper motions referred to the mean pole and mean equinox

### - ICRF –

- realized by barycentric directions of extragalactic objects

*(precision = 0.4 mas)*

- no proper motions
- no reference to the mean pole and mean equinox

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## Resolutions of the 2000 IAU GA on the celestial reference systems

- IAU Resolution B1.3

### *Definition of BCRS and GCRS*

*Aim: coordinate systems in the framework of GR*

- IAU Resolution B1.6

### *IAU 2000 Precession-Nutation Model*

*Aim: submilliarcsecond accuracy*

- IAU Resolution B1.7

### *Definition of Celestial Intermediate Pole*

*Aim: realization of the pole in the high frequency domain*

- IAU Resolution B1.8

### *Definition and use of CEO and TEO*

*Aim: accurate estimation of parameters : UT1, Precession-nutation separately*

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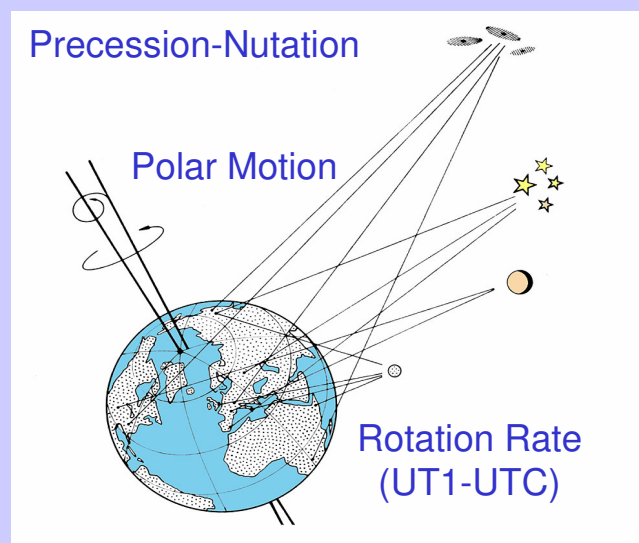
## IAU 2000 Resolution B1.3

Clarification of IAU's 1991 definition of the coordinate systems in the framework of GR : *distinction between the celestial systems*

- a) for Solar System (BCRS) which can be considered to be a *global coordinate system* that contain all the 'far away regions'
- b) for the Earth (GCRS) which can only be considered as a *local coordinate system*

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## Earth Orientation Parameters

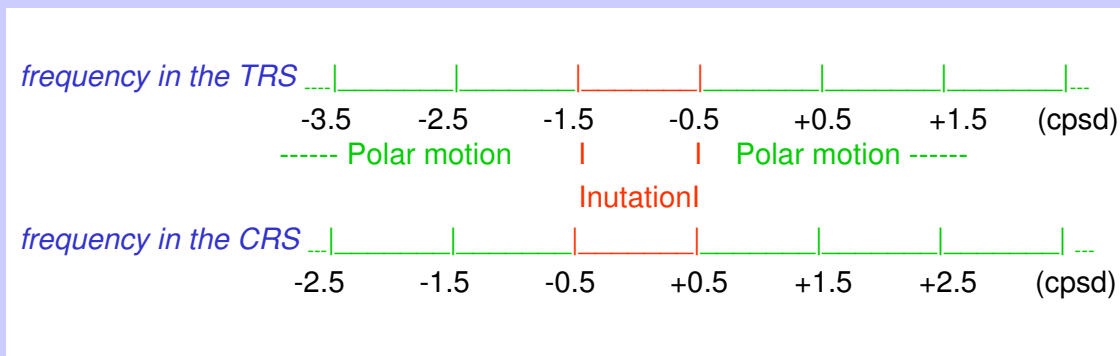


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## Definition of the Celestial Intermediate Pole (IAU Resolution B1.7)

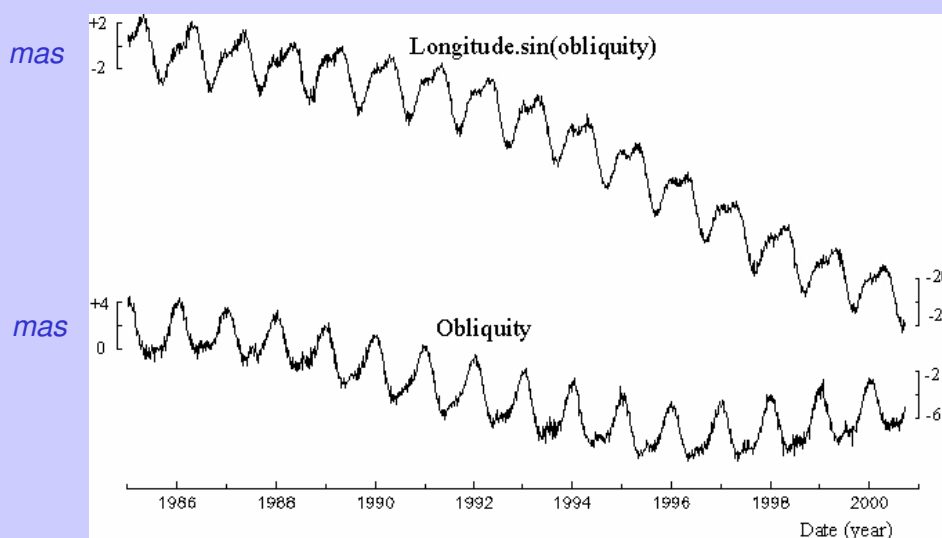
### Definition of the CIP for high frequency variations

- Celestial motion is the IAU 2000 precession-nutation for periods > two days + offsets
- Nutations with periods < two days included in the model for motion in the TRS



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### VLBI estimates of celestial pole offsets w.r.t. the IAU 1976/1980 precession-nutation model



**VLBI provides the actual position of the celestial pole**

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## Implementation of Resolutions B1.6

- *Nutation*

**IAU2000A** : ~ 650 luni-solar terms and ~ 650 planetary terms at 1  $\mu$ as  
IAU 2000 B (its shorter version): ~80 terms for 1 mas level

- *Precession*

**IAU 2000** : IAU 1976 + (VLBI) corrections to precession rates

$$d\psi_A \text{ (IAU 2000)} = - 0''.29965/\text{cy} \quad ; \quad d\omega_A \text{ (IAU 2000)} = - 0''.02524 /\text{cy}$$

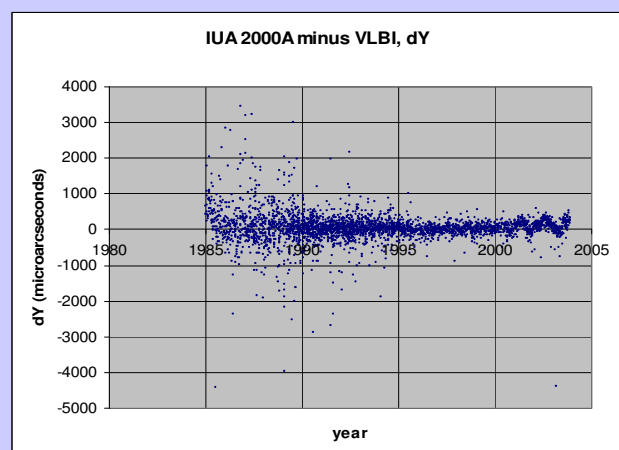
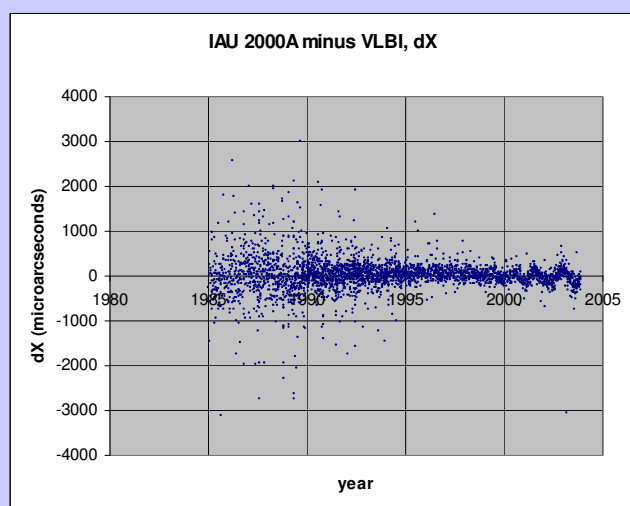
- *Celestial pole offsets at J2000*

**IAU 2000** frame biases (VLBI estimates)

$$\xi_0 \text{ (IAU 2000)} = - 16.6 \text{ mas} \quad ; \quad \eta_0 \text{ (IAU 2000)} = - 6.8 \text{ mas}$$

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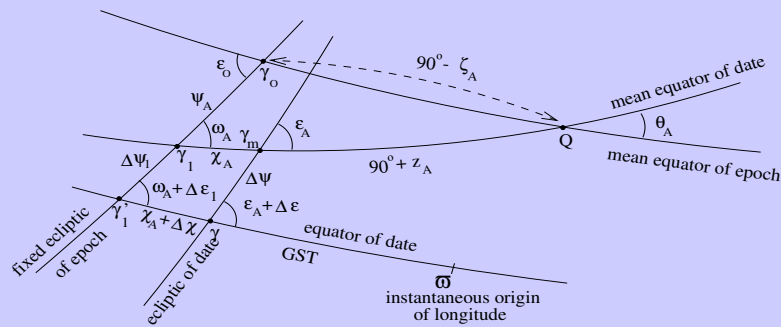
## VLBI celestial pole offsets w.r.t. the IAU 2000 precession-nutation model



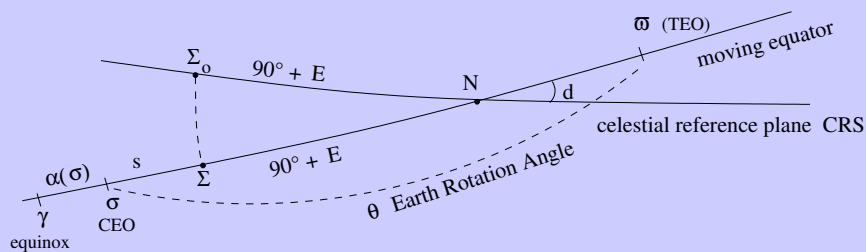
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## Implementation of Resolutions B1.8

### Classical transformation: equinox-based

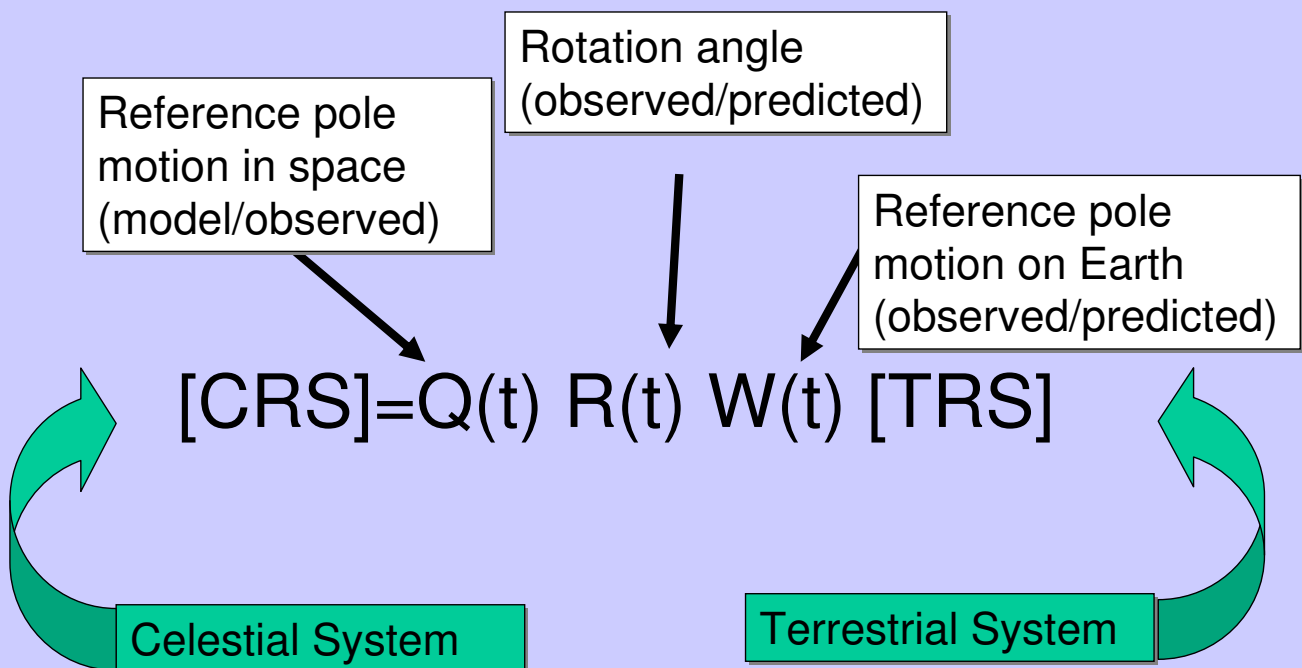


### Recommended new transformation: CEO based



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## Transforming Coordinates



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## Motion of the Pole in the Terrestrial System

### “Old”

$$W(t) = R_1(y_p)R_2(x_p)$$

- $x_p$  and  $y_p$  provided by IERS

### “New”

$$W(t) = R_3(-s')R_1(y_p)R_2(x_p)$$

$$s' = -0.0015 \left( \frac{a_c^2}{1.2} + a_a^2 \right) t$$

- same  $x_p$  and  $y_p$
- corrections for ocean tides
- short-period nutations
- $a_c$  and  $a_a$ : average amplitudes of Chandler and annual polar motions

**Software** at <http://maia.usno.navy.mil/ch5subs.html>

SP2000 subroutine produces  $s'$

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## Earth Rotation Angle

### “Old”

$$R(t) = R_3(-\text{GST})$$

- GST computed using UT1-UTC from IERS
- Tidal corrections to UT1
- **GST referred to the equinox**

### “New”

$$R(t) = R_3(-\theta)$$

- $\theta$  computed using same UT1-UTC
- Same tidal corrections
- **$\theta$  referred to the CEO**

**Software** at <http://maia.usno.navy.mil/ch5subs.html>

ERA2000 subroutine produces the Earth rotation angle  $\theta$

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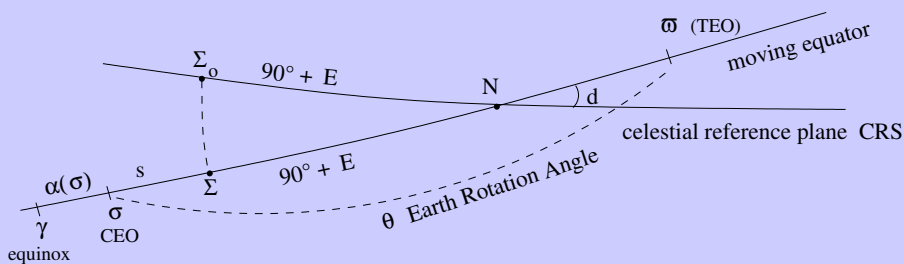
## Change of the origin on the intermediate equator

### Using CEO/CIO

- ERA** =  $\theta = k \text{ UT1}$  ;  $d\theta/dt = \omega_3$
- “intermediate” right ascensions** referred to the CEO/CIO

### Using equinox (with implicit use of CEO/CIO)

- Sidereal time** =  $\theta (\text{UT1}) + \text{“equation of the origins”}$   
= GMST (UT1, TT) + **“equation of the equinoxes”**
- right ascensions** referred to the true equinox



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## Motion of the Pole in the Celestial System

### “Old”

$$Q(t) = [P][N]$$

$$[P] = R_3(\zeta_A) R_2(-\theta_A) R_3(z_A)$$

$$[N] = R_1(-\varepsilon_A) R_3(\Delta\psi) R_1(\varepsilon_A + \Delta\varepsilon)$$

where all quantities are provided as a function of time

- Free-core nutation model available from IERS

### “New”

$$Q(t) = \begin{pmatrix} 1 - aX^2 & -aXY & X \\ -aXY & 1 - aY^2 & Y \\ -X & -Y & 1 - a(X^2 + Y^2) \end{pmatrix} \cdot R_3(s)$$

where X and Y are functions of time, and

$$a = \frac{1}{2} + \frac{1}{8}(X^2 + Y^2)$$

$$s = \int_{t_0}^t a \left( \frac{dX}{dt} Y - X \frac{dY}{dt} \right) dt$$

- Same free-core nutation model

**Software** at <http://maia.usno.navy.mil/ch5subs.html>

- XY2000A subroutine provides X, Y, s
- BPN2000 subroutine provides bias-precession-nutation matrix
- IAU2000A available at <ftp://maia.usno.navy.mil/conv2000/chapter5/IAU2000A.f>.
- IAU2000B is available at <ftp://maia.usno.navy.mil/conv2000/chapter5/IAU2000B.f>

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## Post-2003 rigorous transformation (microarcsecond level)

- B : Bias : CRS  $\rightarrow$  mean matrix at epoch  $(\xi_0, \eta_0, d\alpha_0)$
- P : Precession
- N : Nutation *IAU 2000A*

### CEO-based (New) transformation

Q(X, Y, s) includes bias + precession + nutation + cross terms  
 $\rightarrow$  intermediate system

### Equinox-based (Classical) transformation

B P N: product of 3 transformations for (i) bias, (i) precession, (iii) nutation  
 $\rightarrow$  true equator and equinox

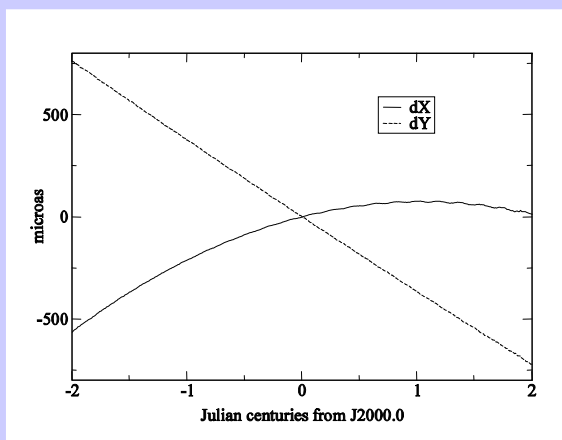
### Further improvements

- (i) IAU WG "Precession and the ecliptic"
- (ii) IAU WG "Nomenclature for fundamental astronomy"

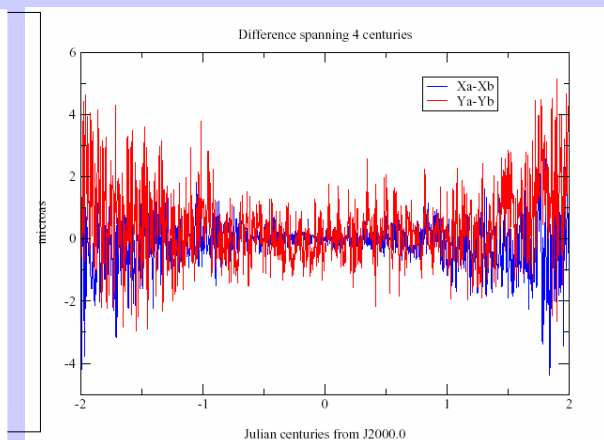
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## Differences in the X, Y celestial position of the pole

*period 1800- 2200*



*post-2003 - pre-2003 procedures*

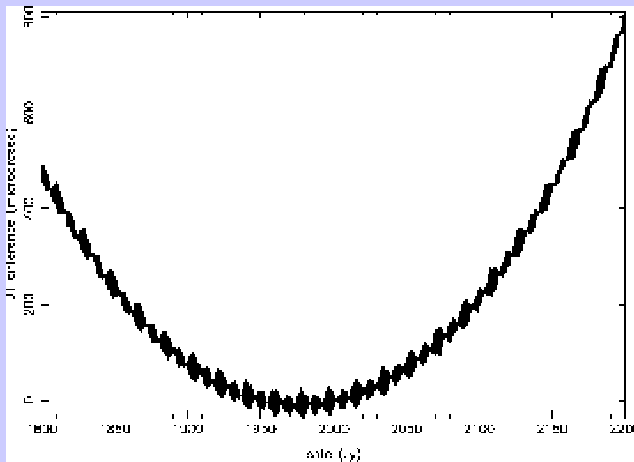


*CEO-based - rigorous equinox-based*

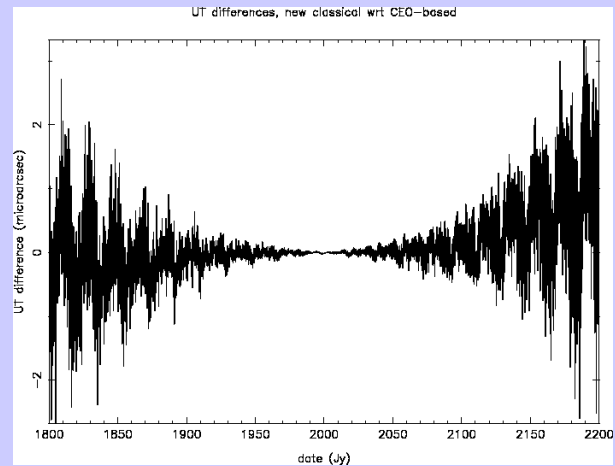
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## Differences in UT1

period 1980-2020



post-2003 - pre-2003 procedures



CEO-based - rigorous equinox-based

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## Concluding remarks

- *IAU 2000 recommendations bring significant improvements in the*
  - definition of the International Celestial Reference System
  - procedures to be used in its realization
- *The IAU recommendations include*
  - an improved precession-nutation formulation
  - more rigorous definitions of the pole and equatorial origin of the reference system
- *The consequences for the whole astronomical community are*
  - improvement of the IAU precession-nutation model,
  - a new definition of Universal Time and its relationship to sidereal time
  - the abandonment of the intermediary reference to the ecliptic and equinox
- *The International Earth Rotation Service (IERS)*
  - has implemented these recommendations
  - provides the data necessary to implement the previous definitions

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