

# On the possible detection of inter-annual deformation signal at the Earth's surface due to the fluid core dynamics

Length-Of-Day variations and Torsional waves

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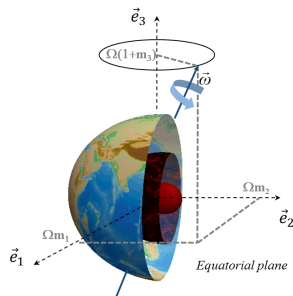
Journées 2019 - Astrometry, Earth Rotation and Reference Systems  
in the Gaia era

# LOD changes

In terrestrial reference system,

$$\omega = \Omega(m_1, m_2, 1 + m_3)$$

$$\Delta LOD = -\overline{LOD} m_3$$



Processes	Time scale	Amplitude
Tidal friction, GIA, present-day ice melting, tectonics, etc.	secular	$< 2 \text{ ms/cy}$
Core-Mantle interactions	decadal	$\sim 2 \text{ ms}$
Atmospheric, oceanic and hydrologic	interannual	$\sim \text{ms}$
Core-Mantle interactions	interannual ( $\sim 6 \text{ yr}$ )	$\sim 0.12 \text{ ms}$
Atmospheric, oceanic and tides	seasonal	$\sim 0.5 \text{ ms}$
Tides	monthly & fortnightly	$\sim 0.5 \text{ ms}$

# A 5.9-yr oscillation in LOD

Abarca del Rio et al. 2000; Holme & de Viron (2013)

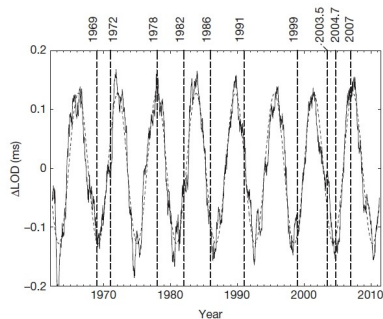
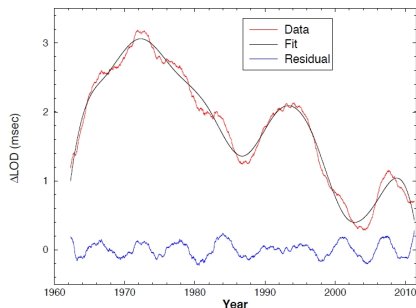


Figure 2 | Decadally detrended LOD data (with 6-month running average), plotted with 5.9-year oscillation fit (dashed line). Vertical lines show best determinations of geomagnetic jerk timings.

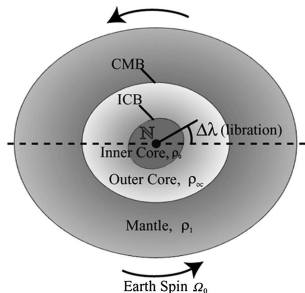
Holme & de Viron (2013)

↓  
5.9-year oscillation

# A 5.9-yr oscillation in LOD: Mechanism?

## Mantle-Inner Core Gravitational coupling (MICG)

Buffett (1996, 1997), Mound & Buffett (2006)

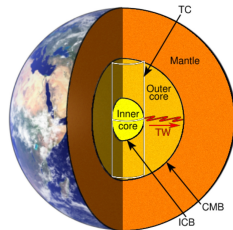


Chao (2017)

Unlikely alone: strength of gravitational coupling too small (Davies et al. 2014)

## Torsional waves

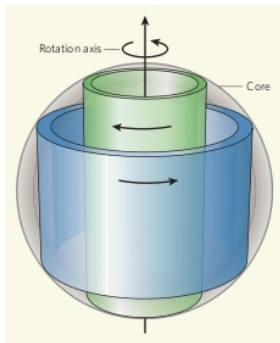
Gillet et al. (2010; 2017)



Teed et al. (2019)

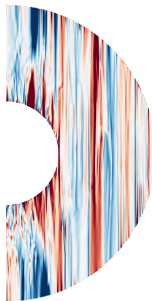
→ Traveling Waves break upon CMB

# Core-Mantle Angular Momentum exchanges



axial invariance (quasi-geostrophy)  
in numerical geodynamo simulation

Schaeffer et al. (2017)



if axially invariant : only concern  $t_1^0$   
and  $t_3^0$  "zonal" coefficients

Jault et al. (1988); Jackson et al.  
(1993); Jault & Finlay (2015)

# Core-Mantle Angular Momentum exchanges

Variations in core angular momentum caused by time changes of geostrophic velocity are compensated by variations in mantle angular momentum and thus in LOD.

- Geostrophic flow velocity:

$$U_G = - \sum_{n=0}^{\infty} t_{2n+1}^0 P_{2n+1}$$

- Core angular momentum ( $C_c$  core moment of inertia):

$$H_c \simeq C_c (t_1^0 + 1.776t_3^0 + 0.0796t_5^0 + 0.002t_7^0 + 4.10^{-5}t_9^0 + \dots),$$

- Conservation of total angular momentum of Earth:

$$\rightarrow \Delta LOD = -H_c \frac{2\pi}{\Omega^2 C_m} \simeq 1.232 (\delta t_1^0 + 1.776\delta t_3^0)$$

(LOD in ms, flows in km/yr)

Jault & Finlay (2015)

# Inter-annual LOD changes and core flows

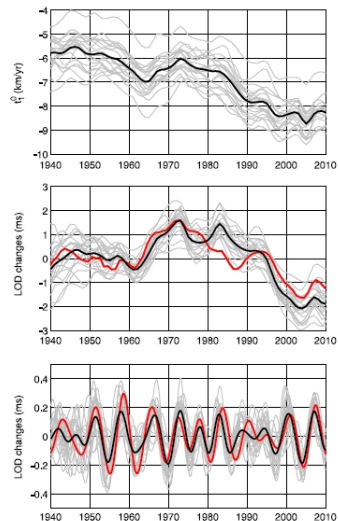
(top) Flow coefficient  $t_0^1$  (km/yr)

(middle) predicted (black) and observed LOD changes (red) (ms)

(bottom) LOD band-pass filtered between 4 and 9.5 years.

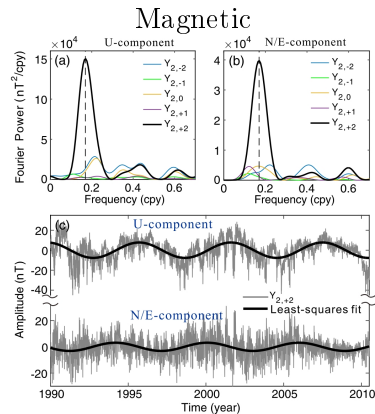
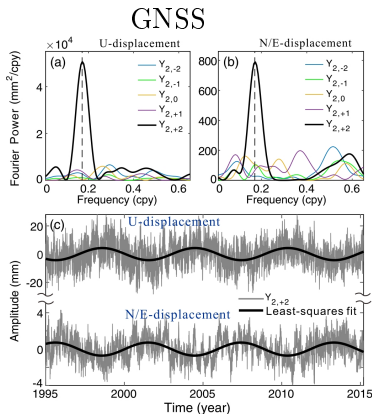
→ inter-annual LOD changes well-explained by core flow models inverted from (independent) geomagnetic data

(Gillet et al. 2015)



# A 5.9-year signal in GNSS and magnetic data?

Ding & Chao (2018):  $Y_2^2$  pattern, linked to MICG coupling



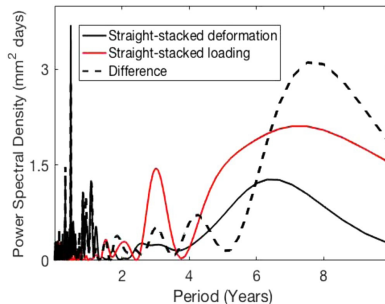
amplitudes a few mm (on  $Z$ ) and 5-10 nT (on  $B_r$ ) (Ding & Chao 2018)



# A 5.9-year signal in GNSS data?

Watkins et al. (2018):

- stacked spectra (BUT only 12-years of time-series)
- a 5.9-year signal detected in GNSS data but not conclusive



- Is the observed 5.9-yr oscillation compatible with core flows models?
- Can we reproduce previous results?

# Surface deformation and core flows

- vertical displacement at the Earth's surface:

$$u_r = \sum_n \bar{h}_n \frac{\Delta P_n}{\rho g_0},$$

- $\bar{h}_n$  degree- $n$  Love numbers ( $h_2, h_4, h_6$ )  $\simeq (0.23, 0.05, 0.01)$
- geostrophic pressure  $\Delta P_n = 2\rho_c \Omega U_n L_n$ , with  $L_n \simeq 2\pi r_c / (2n + 1)$

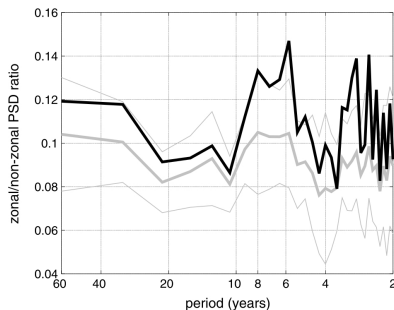
Ding & Chao (2018):

- vertical surface displacement of  $4.3 \pm 1.7$  mm  $\rightarrow \Delta P \sim 1000$  Pa  
 $\rightarrow U_Z \sim 10^{-4}$  m/s  $\sim 3$  km/yr

... good order of magnitude?

# Zonal and non-zonal motions

Only **zonal toroidal** motions of the core wrt mantle contribute to axial component of angular momentum of the core.



$$|U_{NZ}| = O(2) \text{ km/yr}$$

$$|U_Z| = O(0.6) \text{ km/yr}$$

$$\rightarrow |U_{NZ}| \approx 3|U_Z|$$

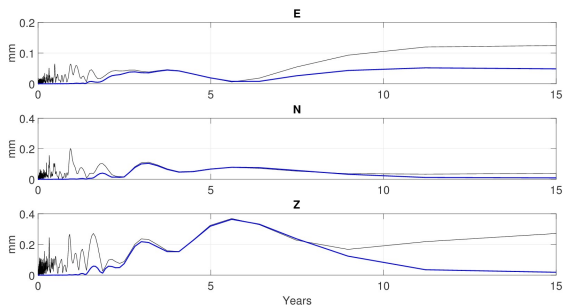
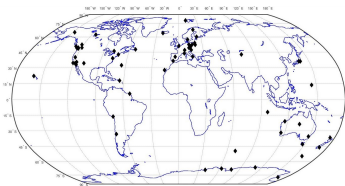
(Gillet et al. 2015)

5.9-year oscillation: weak in zonal flows (torsional waves), absent in non-zonal flows

→ do not expect strong 5.9-year signal: 0.2-1 mm vertical displacement

# GNSS data analysis: vertical displacement

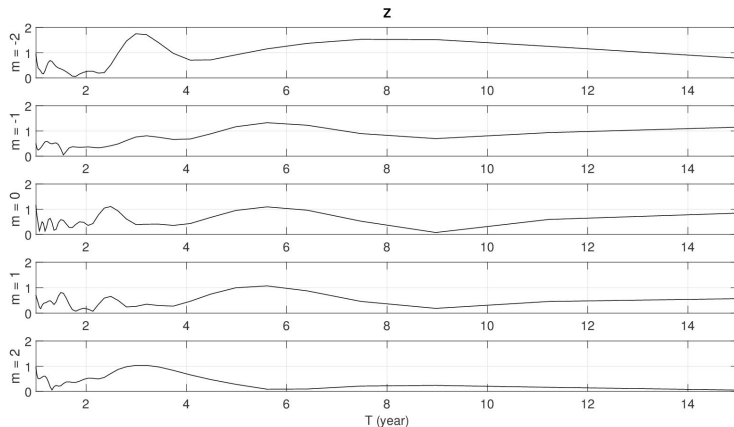
International GNSS Service (IGS) solutions from 2nd data reprocessing campaign in ITRF2014 with geophysical corrections (tides, ocean loading, non-tidal atmospheric loading) after IERS Conventions (2010) (Rebischung et al. 2016)



Stacked FFT of solutions from 63 stations with duration 18.5 years (band-pass filtering [2 - 12] yr)  $\rightarrow$  0.4 mm on Z at  $\sim$  6-year

# GNSS data analysis: vertical displacement

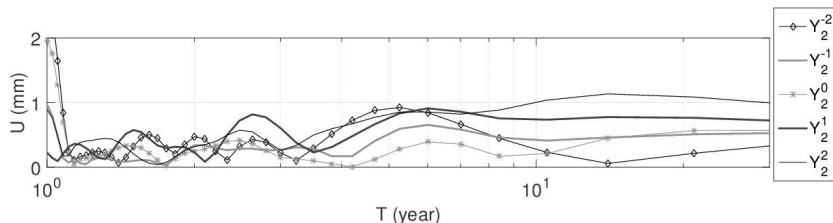
Optimal Sequence Estimate as in Ding & Chao (2018) applied on IGS Repro2 solutions from 63 stations with duration 18.5 years



# GNSS data analysis: vertical displacement

Peak at 6-year period in hydrological loading predictions?

↓ 6 year



Optimal Spectral Estimate on GLDAS predictions at GNSS sites

<http://loading.u-strasbg.fr/>

→ 1 mm vertical displacement at 6-year in GLDAS predictions

# Summary

- 6-year oscillation in LOD well-explained by torsional waves in fluid core
- if detected 6-year oscillation in vertical GNSS data originates from fluid core, then associated core flows of the order of 3 km/yr ( $\gg$  0.6 km/yr from torsional waves obtained from geomagnetic observations)
- if  $Y_2^2$  pattern confirmed, then **non-zonal** flows should play a major role, but no peak at 6-year period in reconstructed non-zonal flows
- even with non-zonal flow 3 to 5 times larger than zonal flows, associated pressure flows (in quasi-geostrophic approximation) similar to zonal ones  
→ **not enough to induce 1-mm vertical displacement at surface**
- our attempts have not yet confirmed previous detection: a peak present at  $\sim$  6-year with amplitude 0.4 mm
- but hydrological loading signal also has a peak at  $\sim$  6-year with similar amplitude...
- effect on polar motion known to be small (e.g. Dumberry (2008); Greff-Lefftz & Legros (1995))...

# Acknowledgments

Thank you for your attention