

# RETRIEVING DIURNAL AND SEMIDIURNAL SIGNALS IN POLAR MOTION AND UT1 FROM ANALYSIS OF THE ROUTINE VLBI OBSERVATIONS

Aleksander Brzeziński<sup>1</sup> and Sergei Bolotin<sup>(2,1)</sup>

<sup>1</sup> Space Research Centre, Polish Academy of Sciences  
Bartycka 18A, 00-716 Warsaw, Poland  
alek@cbk.waw.pl

<sup>2</sup> Main Astronomical Observatory, National Academy of Sciences of Ukraine  
Akad. Zabolotnogo Str. 27, 03680 Kiev, Ukraine  
bolotin@mao.kiev.ua

Presented at

*XXVIth General Assembly of the International Astronomical Union*  
*Prague, Czech Republic, 14–25 August 2006*  
*Joint Discussion 16*

---

A.B. wishes to express his sincere thanks for the IAU grant to attend the IAU General Assembly. The research of S.B. has been supported by the post-doc visiting grant in a frame of the “Descartes-Nutation” project.

# Overview

---

1. Introduction
2. Parametrization of polar motion and UT1
3. Analysis of VLBI observations
4. Results
5. Conclusions

## Introduction

---

Diurnal and subdiurnal signals in polar motion (PM) and UT1:

- **Tidal effects:** regular and predictable, harmonic models provided by the IERS Conventions (2003), Tables 5.1, 8.2a,b and 8.3a,b
  - Influence of the gravitationally forced ocean tides with diurnal and semi-diurnal periods; amplitudes up to 300  $\mu\text{s}$
  - Direct influence of the tidal gravitation on the triaxial structure of the Earth, diurnal in PM, semidiurnal in UT1; amplitudes up to 30  $\mu\text{s}$
- **Geophysical signals:** irregular or quasi-harmonic, adequate representation by time series; expected total amplitude between 10 and 30  $\mu\text{s}$ 
  - Atmospheric and nontidal oceanic influences:  $S_1/S_2$  components with periods 24/12 hrs and their side lobes generated by seasonal modulations
  - Atmospheric normal modes  $\psi_1^1, \xi_2^1$  with central periods of 1.2, 0.6 days, respectively

## Introduction (cont.)

---

Modeling efforts and observational evidence

- Concern mostly the purely harmonic ocean tide influence which is dominant effect in diurnal and semidiurnal bands
  - **Ocean tide model**: hydrodynamic model constrained by T/P altimetry observations (Chao et al., 1996), recommended by IERS Conventions (2003)
  - **VLBI solutions**: (Sovers et al., 1993; Herring & Dong, 1994; Gipson, 1996)
  - **SLR solution**: (Watkins & Eanes, 1994) with later updates by R. Eanes
  - **GPS solution**: (Rothacher et al., 2001)
- Geophysical signals
  - Estimated in most of the space-geodetic solutions cited above, but deeper analysis done only in case of GPS
  - Continuous observation campaigns, like CONT94, CONT02, CONT05
  - Estimation from high-resolution atmospheric/oceanic excitation data

## Introduction (cont.)

---

### Our purpose:

- To extract from the routine VLBI observations the high-frequency (diurnal, semidiurnal, ...) signals in polar motion and UT1, which can be used for constraining the tidal models and for time domain comparisons with the available geophysical excitation data.

### The method:

- Proposed originally by Herring and Dong (1994) and further developed by Mathews and Herring (2000), Brzeziński (1994; 2000), relies upon the so-called **complex demodulation** technique.

# Parametrization of polar motion and UT1

---

## Polar motion

$$p(t) = x(t) - iy(t) = \sum_{\substack{\ell=-N \\ \ell \neq -1}}^N [x_\ell(t) - iy_\ell(t)] e^{i\ell\phi}$$

or, equivalently

$$\begin{bmatrix} x(t) \\ y(t) \end{bmatrix} = \sum_{\substack{\ell=-N \\ \ell \neq -1}}^N \left\{ \begin{bmatrix} x_\ell(t) \\ y_\ell(t) \end{bmatrix} \cos(\ell\phi) + \begin{bmatrix} y_\ell(t) \\ -x_\ell(t) \end{bmatrix} \sin(\ell\phi) \right\}$$

## Universal time

$$\text{UT1}(t) = \sum_{\ell=0}^N [u_\ell^s(t) \sin(\ell\phi) + u_\ell^c(t) \cos(\ell\phi)]$$

where  $i = \sqrt{-1}$  denotes imaginary unit,  $t$  – time, and  $\phi = \text{GMST} + \pi$

## Parametrization of polar motion and UT1 (cont.)

---

### Assumption

- $x_\ell(t), y_\ell(t), u_\ell^s(t), u_\ell^c(t)$  do not vary significantly during the observing session  
(in computations we estimate them as constant during one 24-hour session)

### Remarks

- ⇒ in standard estimation of EOPs from VLBI observations  $N = 0$  that is the summation for both PM and UT1 reduces to one term only (with  $\ell = 0$ )
- ⇒  $\ell = 0$  :  $p_o(t) = x_o(t) - iy_o(t)$  and  $u_o^c(t)$  are the long periodic components of polar motion and UT1
- ⇒  $\ell = 1, 2, \dots$  : the  $\ell$ -th term expresses quasi diurnal, semidiurnal,  $\dots$  variations in polar motion (retrograde/prograde for  $-/+$ ) and in UT1
- ⇒  $\ell = -1$  : this term of polar motion is not included in the expansion because it is parameterized as nutation (the celestial pole offsets)

# Parametrization of polar motion and UT1 (cont.)

Assume for simplicity the regular time distribution of VLBI sessions, with a separation of  $k$  days. The frequency domain of  $x_\ell(t)$ ,  $y_\ell(t)$ ,  $u_\ell^S(t)$ ,  $u_\ell^C(t)$  is limited to the Nyquist interval

$$\left(-\frac{1}{2k}, +\frac{1}{2k}\right) \text{ cpd.}$$

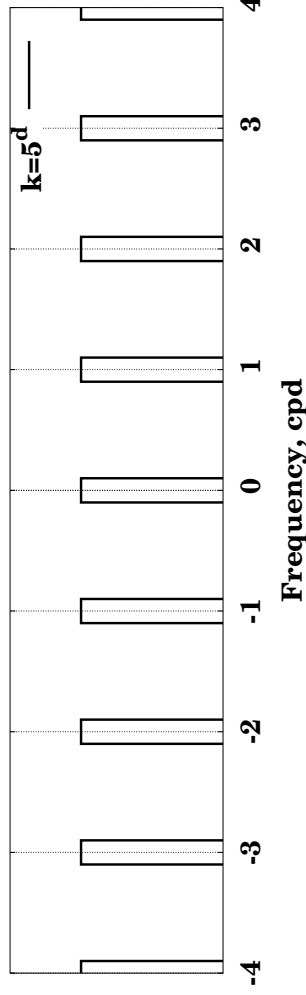
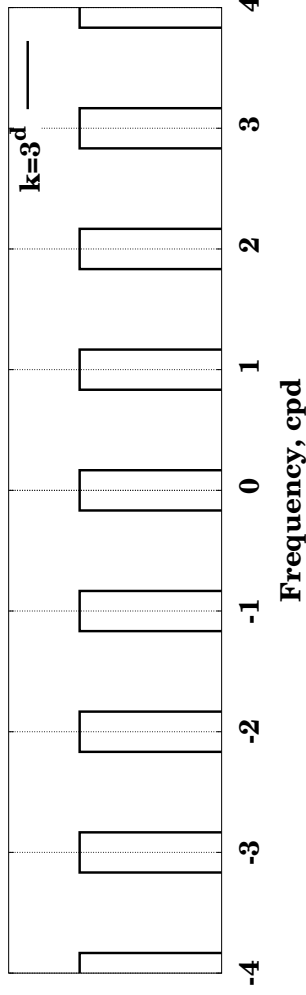
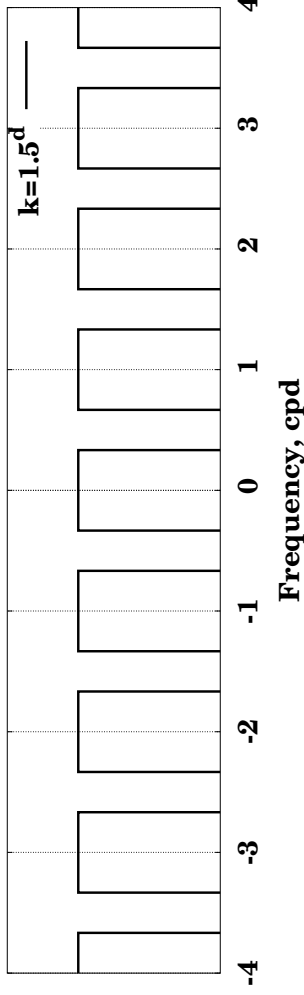
The frequency domain of the total expansion and for

$k=1.5$  days,

$k=3$  days,

$k=5$  days,

is shown in the figures.



# VLBI data analysis

---

## VLBI data:

- From 1984.0 till February 2006
- 2,790 VLBI sessions, 4,698,363 dual frequency delays
- 2078 radio sources, 109 stations

## Models:

- IERS Conventions (2003)
- Ocean and atmospheric pressure loading (Petrov and Boy, 2003)

## Software:

- STEELBREEZE

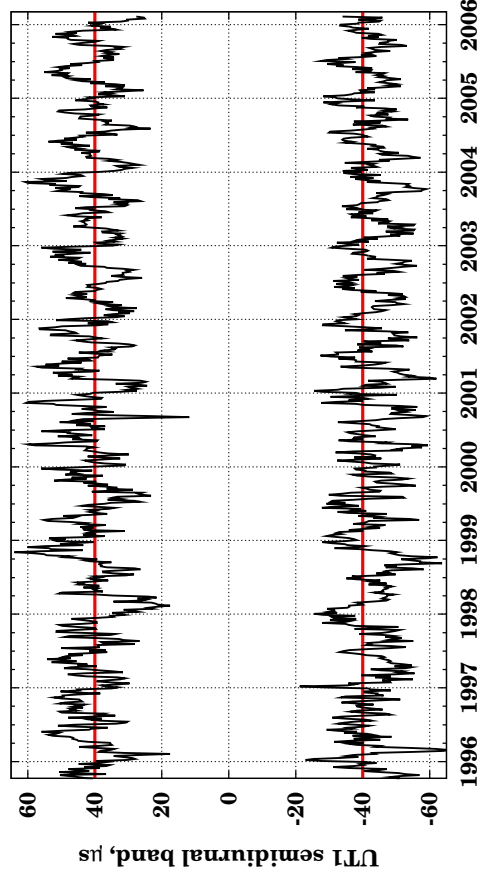
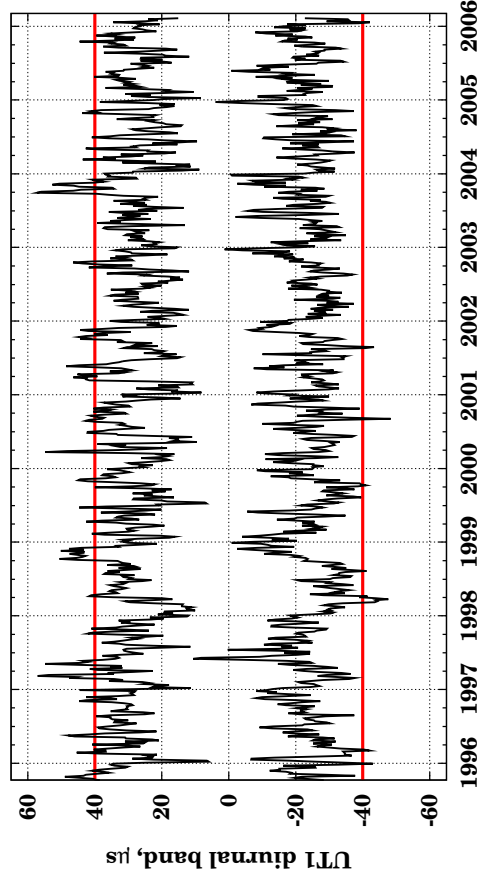
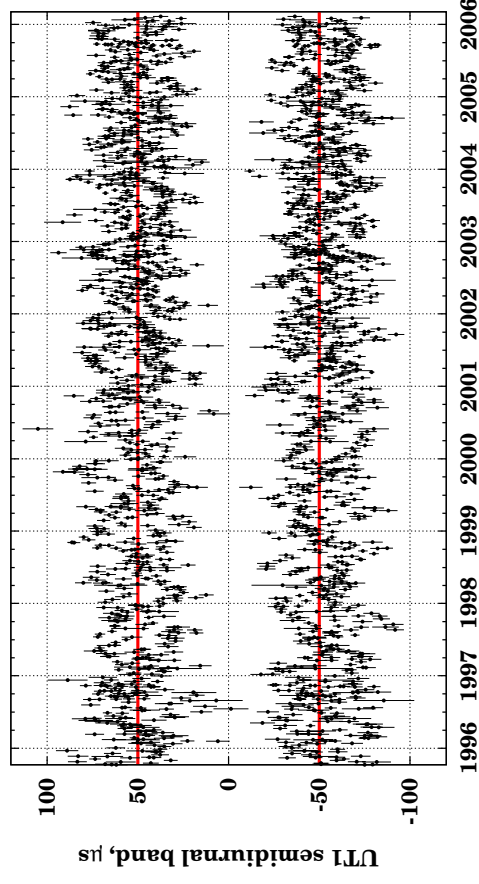
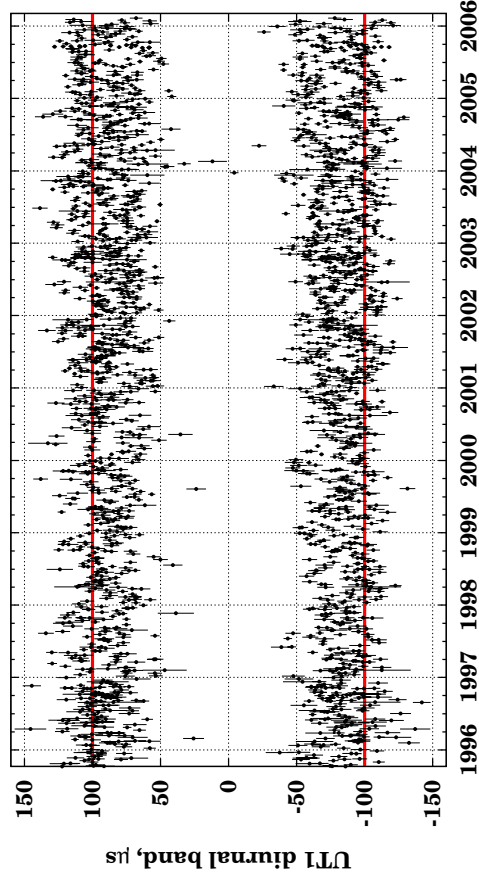
## Estimated parameters:

- global parameters: coordinates of radio sources, positions and velocities of VLBI stations
- local parameters: CIP offset  $[dX, dY]$ ,  $[x_\ell(t), y_\ell(t)]$  and  $[u_\ell^c(t), u_\ell^s(t)]$ , for  $|\ell| \leq 10$
- stochastic parameters: station clock function, wet zenith delay and its gradients

## For consistency check two runs were performed:

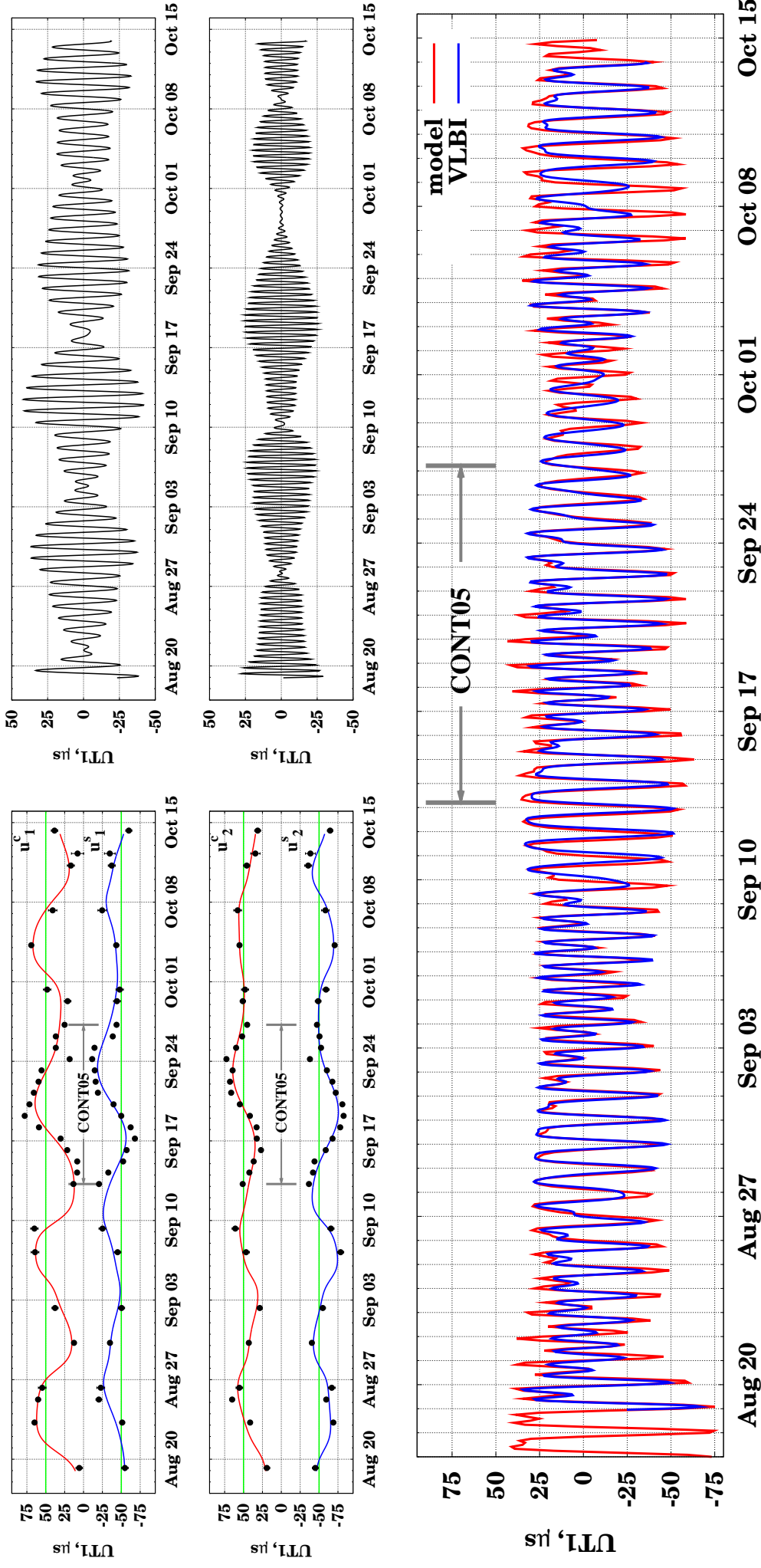
- with a priori model of diurnal/semidiurnal ocean tide variations
- without a priori model

# Results



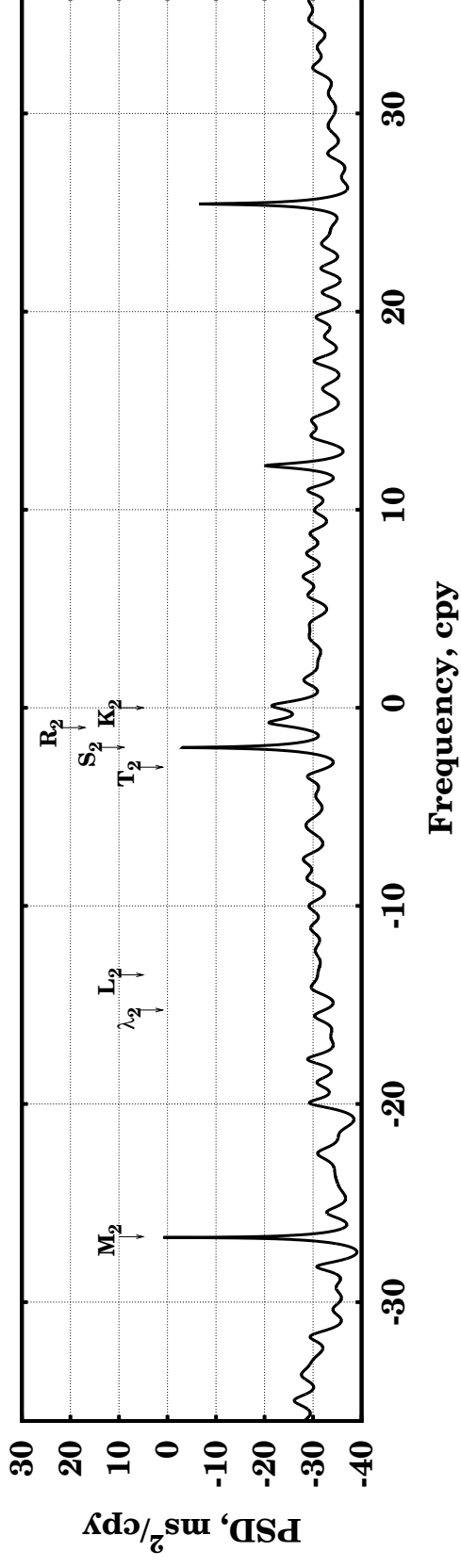
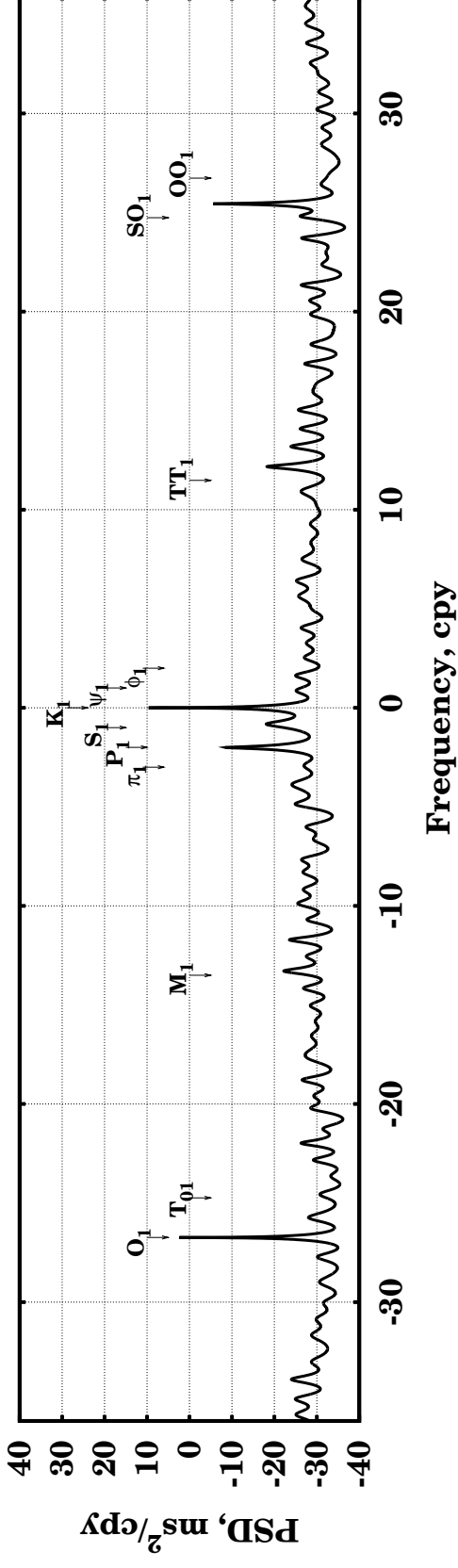
UT1 diurnal (left) and semidiurnal (right) components demodulated from VLBI data, row estimates (top) and smoothed values (bottom)

# Results (cont.)



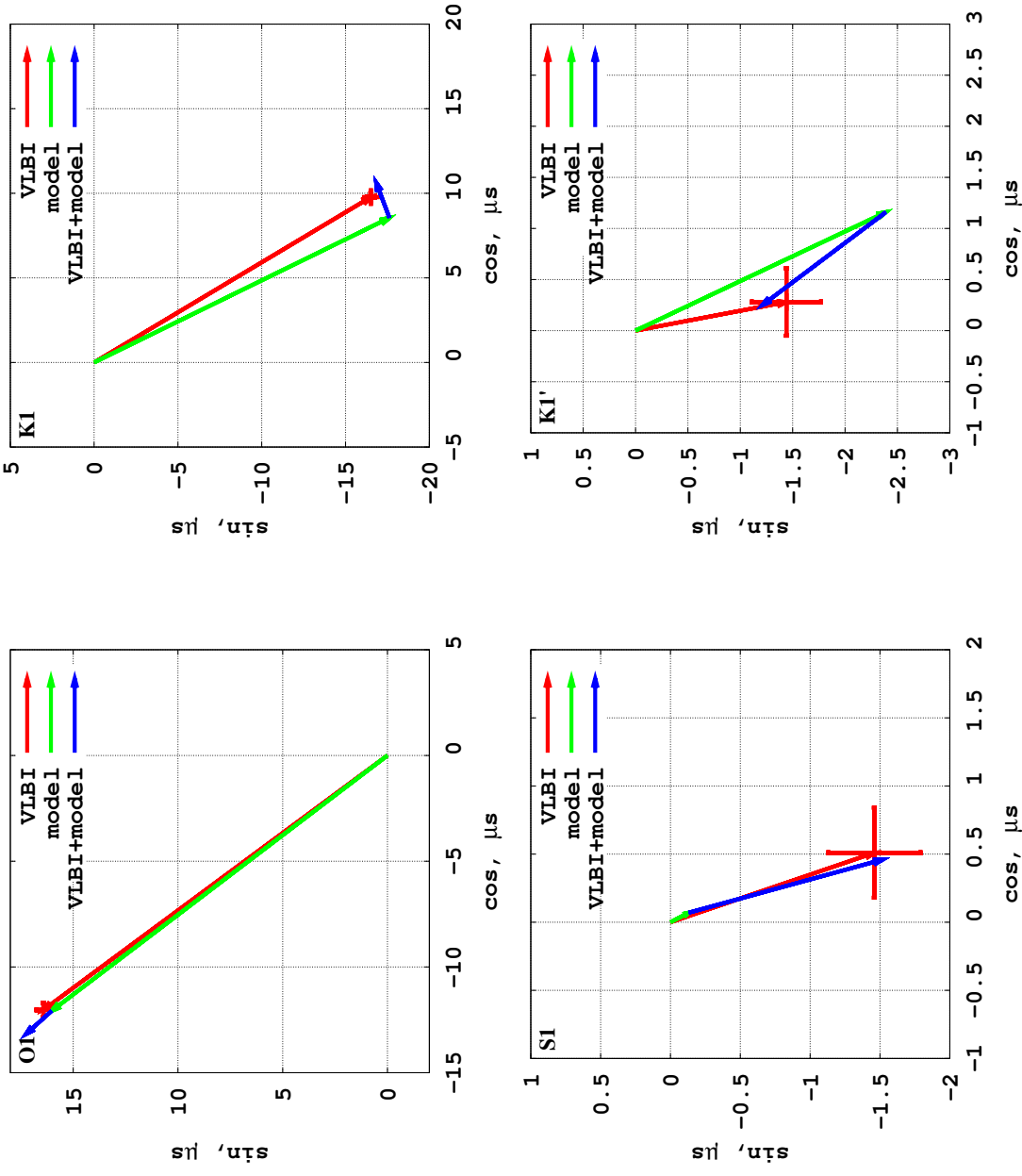
UT1 diurnal and semidiurnal components, estimation from VLBI observations (upper plots) and comparison with the modeled ocean tide effect (lower plot)

## Results (cont.)



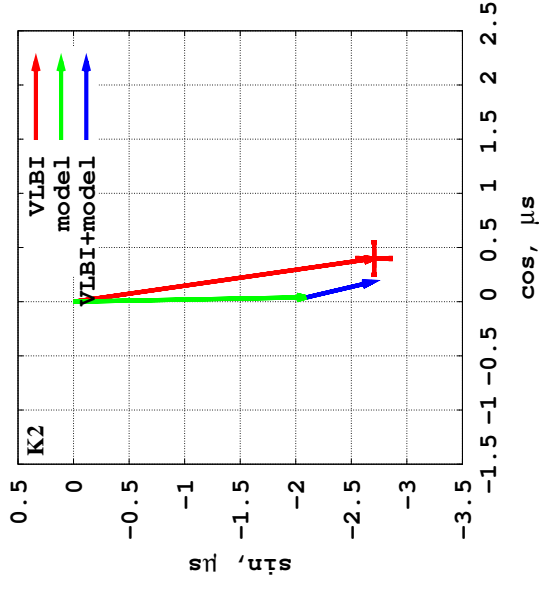
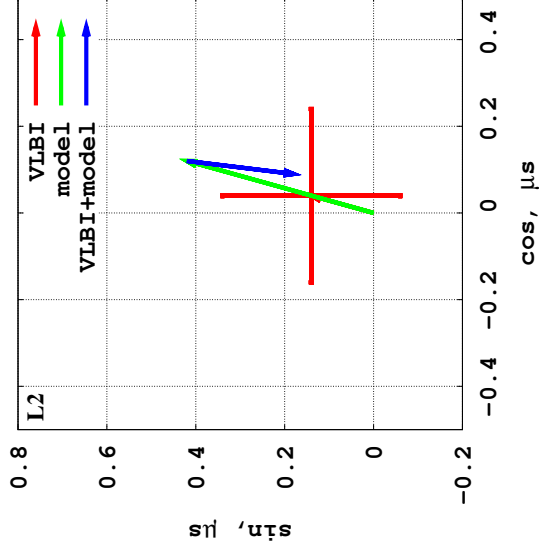
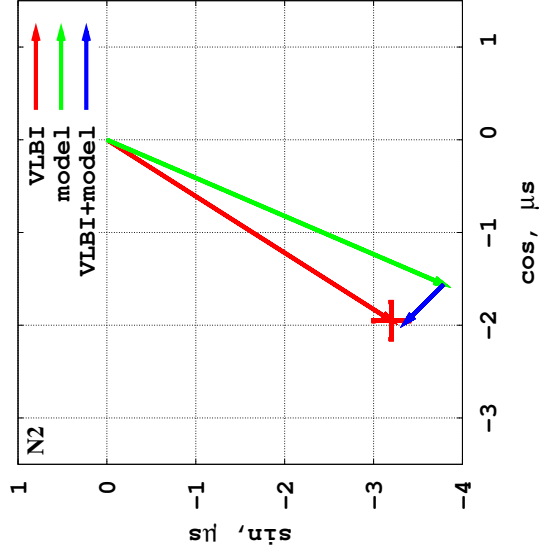
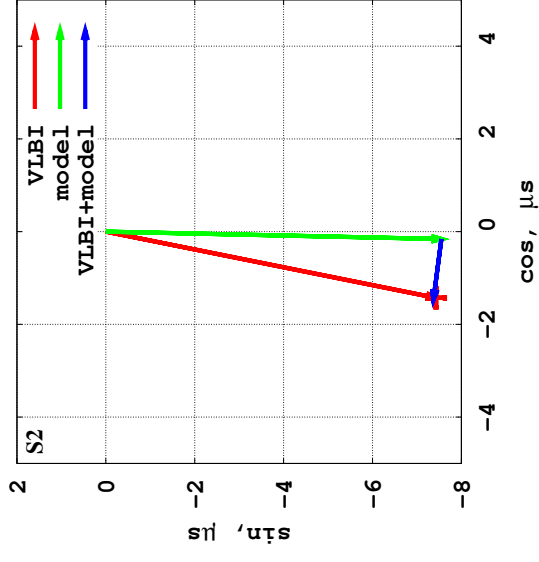
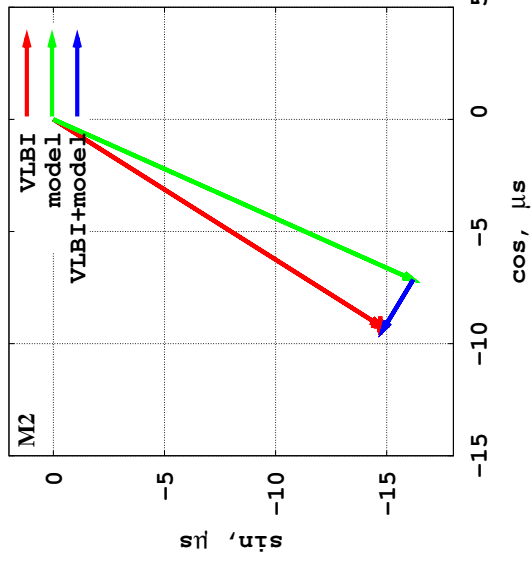
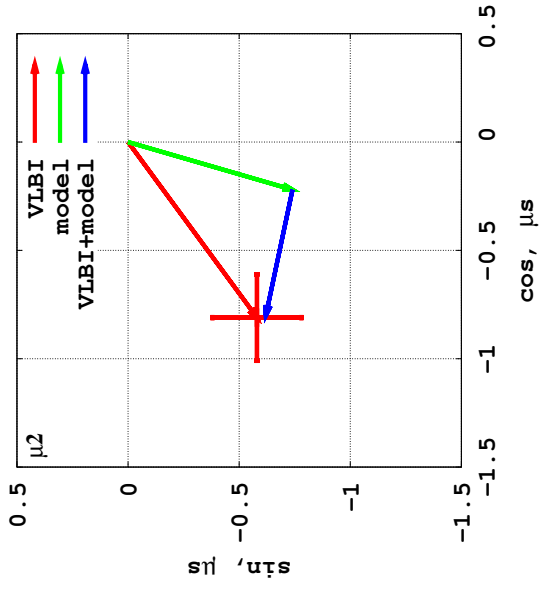
Power spectrum of UT1 variations: diurnal (top) and semidiurnal (bottom).  
Model of the ocean tide variations has been not removed in the estimation.

## Results (cont.)



Diurnal UT1 variations: VLBI estimates vs. modeled ocean tide influence.

# Results (cont.)



Semidiurnal UT1 variations: VLBI estimates vs. modeled ocean tide influence.

---

## Conclusions

- Parametrization implemented in this work enables derivation of the high frequency signals in PM and UT1 from the routine VLBI observations.
- Spectral analysis showed that the estimated time series expressing diurnal and semidiurnal variations describe adequately real physical signals, however  
⇒ we discovered significant differences with the model of ocean tide effects.
- At higher frequencies (3, 4, . . . , cpd) the estimated series do not show any nontrivial spectral features therefore can be neglected in the parametrization.
- This research needs continuation:
  - ⇒ comparison with alternative solutions based on different VLBI software or derived from observations by other space geodetic techniques;
  - ⇒ comparison with diurnal and semidiurnal signals extracted from the high resolution atmospheric and oceanic angular momentum data.

## Conclusions

---

- We recommend that the analysis centers which estimate the EOP and EOP rates with at least daily averaging
  - ⇒ will add diurnal and semidiurnal amplitudes of PM and UT1 to the set of the estimated parameters.
  - ⇒ will perform reanalysis of the archived sets of observations using this extended model, in order to recover past behavior of diurnal and semidiurnal signals.
- Conventional model of the ocean tide influences on PM an UT1 should be improved using new data sets from satellite altimetry and from space geodesy.